

# 1 Dipion photoproduction and the $Q^2$ evolution of the 2 shape of the gold nucleus

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Coherent photoproduction of vector mesons is sensitive to the shape of the target nucleus, as probed at four-momentum scale  $Q^2 \propto (M_V/2)^2$ . Previously STAR presented a high-statistics measurement of  $d\sigma_c/dt$  for coherent  $\pi^+\pi^-$  photoproduction in ultra-peripheral gold-gold collisions, and made a two-dimensional Fourier-Bessel (Hanckel) transformation to give the transverse distribution of interactions in the nucleus. Here, we study how  $d\sigma_c/dt$  evolves with  $Q^2$ . We divide the  $\pi^+\pi^-$  signal into three different mass ( $Q^2$ ) bins to measure how  $d\sigma_c/dt$  evolves with dipion mass. Furthermore, we find that the depth of the first diffractive minimum varies with pair mass. We perform a two-dimensional Fourier-Bessel transform to see how the effective transverse distribution of the interactions changes with decreasing pair mass. In the lowest mass bin, the nuclear profile is broader, which is consistent with expectations from saturation models.

*XXVI International Workshop on Deep-Inelastic Scattering and Related Subjects (DIS2018)*

*16-20 April 2018*

*Kobe, Japan*

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### 3 1. Introduction

4 Nuclear shadowing reduces the cross-section for photon-nucleus interactions compared with  
 5 a collection of the same number of independent nucleons. The reduction is often quantified as  
 6 the change in cross-section for a quark-antiquark dipole (the quantum fluctuation of a photon).  
 7 In addition, shadowing affects other observables in the interaction. This can be studied in the  
 8 dipole picture, where an incident photon fluctuates to a quark-antiquark dipole, which then scatters  
 9 elastically from the nucleus, emerging as a real vector meson. For small dipoles, with large  $Q^2$   
 10 (squared 4-momentum transfer), the interactions can be described in terms of quarks and gluons.  
 11 At lower  $Q^2$ , as will be discussed here, individual quarks and gluons are not visible, but nuclear  
 12 shadowing still affects the cross-section [1, 2].

13 Large dipoles tend to interact with the first nucleon that they encounter, on the front face of  
 14 the nuclear target. For sufficiently large dipoles, the nucleus appears as a black disk, with an equal  
 15 interaction probability ( $\approx 1$ ) at all impact parameters. Small dipoles are less likely to interact, and  
 16 thus can penetrate the nucleus. They have an equal probability to interact with all of the nucleons,  
 17 so the interaction sites follow the nuclear density profile. Coherent interactions probe these two  
 18 cases. For coherent elastic scattering (including vector meson photoproduction), one adds the  
 19 amplitudes for scattering off of the individual nucleons  $i$  at positions  $\vec{x}_i$ :

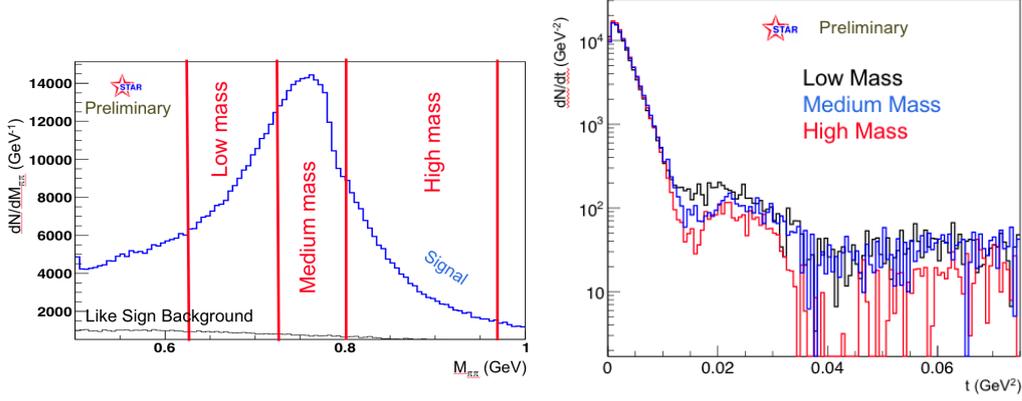
$$\sigma_c = \int d^3\vec{k} |\sum_i A_i \exp(i\vec{k} \cdot \vec{x}_i)|^2 \quad (1.1)$$

20 where (neglecting the small virtuality)  $\vec{k}$  is the momentum transfer from the nucleus to the nascent  
 21 vector meson and  $t = |\vec{k}|^2$ . We take the interaction amplitudes  $A_i$  to be identical. In high-energy  
 22 photoproduction, the longitudinal component  $k_z$  is small, and can be neglected. This also avoids  
 23 the two-fold ambiguity in  $k_z$  due to uncertainty in the photon direction. By measuring  $d\sigma_c/dt$   
 24 and performing a two-dimensional Fourier transform, we can learn about the positions where the  
 25 dipoles interacted within the nucleus [3, 4, 5].

26 Here, we present a study of dipion photoproduction in ultra-peripheral collisions (UPCs) [6].  
 27 In these UPCs, a photon emitted by one nucleus fluctuates to a quark-antiquark dipole which scat-  
 28 ters in the nucleus and emerges as a dipion pair. The final state may be produced via  $\rho$  or  $\omega$   
 29 intermediates, or by direct  $\pi\pi$  photoproduction. These three possibilities interfere, and the combi-  
 30 nation has been shown to provide a good description of the  $\pi\pi$  mass spectrum in the range up to 1  
 31 GeV [5]. The final dipion  $p_T$  comes mostly from the scattering ( $k_T$ ), but also includes a component  
 32 from the photon transverse momentum.

### 33 2. STAR and data selection

34 This analysis uses data taken with the Solenoidal Tracker at RHIC (STAR) detector [7] in  
 35 2010 and 2011, on gold-gold collisions at a center of mass energy of 200 GeV/nucleon pair. For  
 36 this analysis, the most important components of STAR are the time projection chamber (TPC),  
 37 time-of-flight (TOF) system, zero-degree calorimeters (ZDCs) and forward beam-beam counters  
 38 (BBCs). The TPC tracked charged particles with transverse momentum  $p_T > 200$  MeV/c and  
 39 pseudorapidity  $|\eta| < 1$ . The TOF system was used for triggering. The trigger required 2-6 hits in



**Figure 1:** (left) The dipion mass spectrum, showing the three mass bins used in this analysis. The blue curve shows the charge zero pairs, while the black shows the like-sign background. (right)  $dN/dt$  for the three different mass ranges, after subtraction of the incoherent components. The depths of the diffractive minima are different.

40 the TOF system, with  $|\eta| < 1$ , and signals equivalent to 1-4 neutrons in each ZDC. The BBC was  
 41 used to reject events with charged particles with  $2 < |\eta| < 5$ .

42 The analysis used tight cuts to select photoproduced dipion pairs. It selected events with  
 43 exactly two tracks coming from the primary vertex. The tracks had to be well reconstructed, with  
 44 at least 25 space points in the TPC. Track pairs with rapidity  $|y| < 0.03$  were rejected because they  
 45 could be from cosmic-ray muons, which are reconstructed as a pair with  $p_T = 0$  and  $y = 0$ .

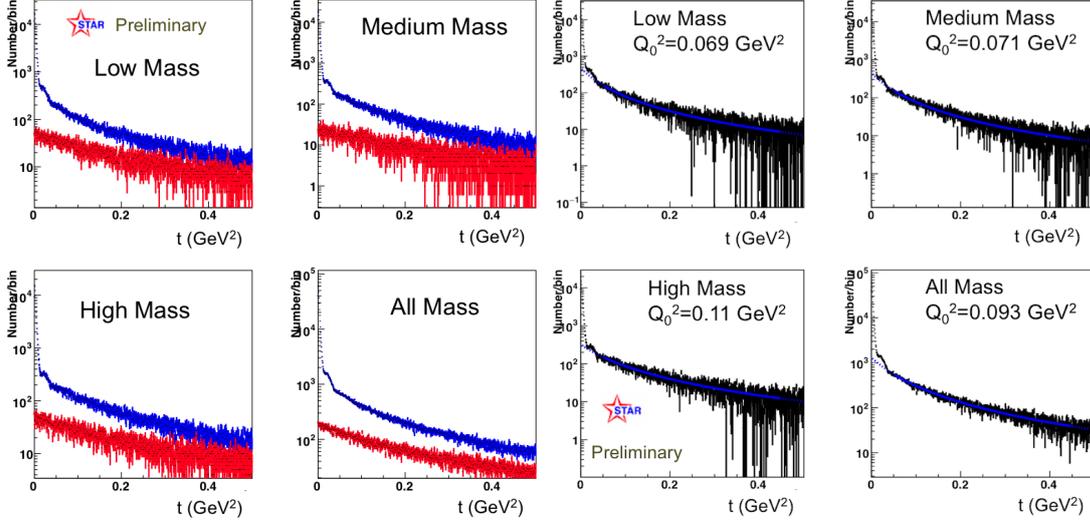
46 This left 437K pairs, with the dipion invariant mass between 620 and 920 MeV. The lower  
 47 edge of the low-mass bin was chosen to largely remove background from two other UPC processes:  
 48  $\gamma\gamma \rightarrow e^+e^-$  and  $\gamma A \rightarrow \omega A$ , followed by  $\omega \rightarrow \pi^+\pi^-\pi^0$ , where the  $\pi^0$  is not seen by STAR. This  
 49 mass spectrum was divided into three ranges with a similar number of events: 149K events (low),  
 50 148K events (medium) and 140K events (high mass). In all three bins, the signal to noise ratio is  
 51 more than 10 : 1.

52 Figure 2 (left) shows the  $t$  spectra of the three mass ranges, along with the like-sign background  
 53 which is an estimate of the background from peripheral hadronic collisions. Figure 2 (right) shows  
 54 the  $t$  distribution of the like-sign subtracted pairs. To remove the incoherent background, we fit the  
 55 histogram in the range  $0.05 \text{ GeV}^2 < t < 0.45 \text{ GeV}^2$  to a dipole function:

$$\frac{dN}{dt} = \frac{A/Q_0^2}{(1+t/Q_0^2)^2} \quad (2.1)$$

56 This is the same function used in Ref. [5], but with a wider fit range. All of the fits have  $\chi^2/DOF \approx$   
 57 1. Ref [5] fixed  $Q_0^2$  to be  $0.099 \text{ GeV}^2$ , while we let it float.  $Q_0^2$  shows some variation with mass  
 58 bin, but the low-mass and medium-mass bins agree within their uncertainties. Some variation of  
 59  $Q_0^2$  with dipole size is not unexpected.

60 As Fig. 2 (right) shows, an exponential does not match the incoherent photoproduction data;  
 61 it would be a straight line on the semi-log plot. For the all-mass bin in the same  $t$  range, an  
 62 exponential fit gives a  $\chi^2/DOF = 1345/639$ , in contrast to the  $\chi^2/DOF = 659/639$  for the dipole



**Figure 2:** (left) The  $dN/dt$  histograms for the three mass bins plus the summed bin. The blue histograms are the net-charge-zero pairs, while the red shows the like-sign background. The coherent production peak is visible for  $t < 0.01 \text{ GeV}^2$ . (right) Like-sign subtracted total  $d\sigma/dt$ . The blue line shows the dipole fit to the data, and the listed  $Q_0$  are from that fit.

63 fit. Although STAR previously used an exponential to model incoherent photoproduction [8, 9],  
 64 with the greatly increased statistics, it is no longer a good fit to the data.

65 The incoherent contribution is then subtracted; the resulting  $d\sigma_c/dt$  is shown in Fig. 1 (right).  
 66 The depths of the first diffraction minima are different for the three curves.

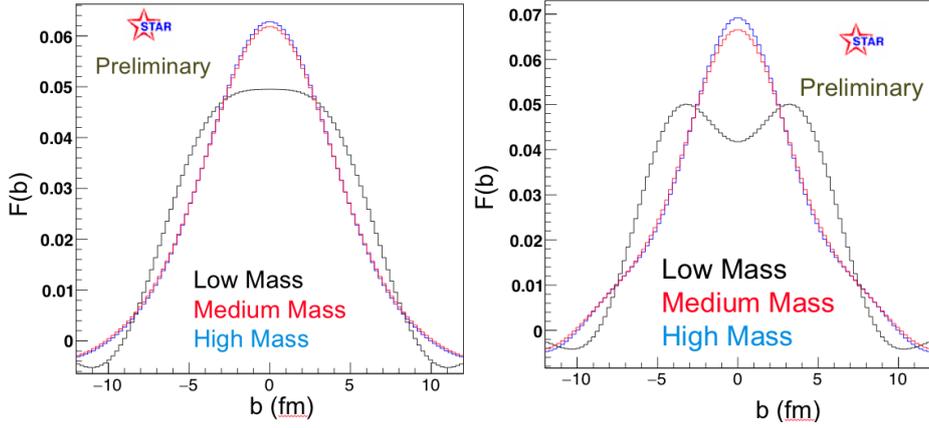
### 67 3. The nuclear shape

68 The two-dimensional nuclear shape profile,  $F(b)$  can be given by observing the two-dimensional  
 69 Fourier-Bessel (Hanckel) transform of  $d\sigma_c/dt$  [3, 4]:

$$F(b) \propto \frac{1}{2\pi} \int_0^{\sqrt{t_{\max}}} dp_T p_T J_0(bp_T) \sqrt{\frac{d\sigma_c}{dt}} \quad (3.1)$$

70 where  $\sqrt{t_{\max}}$  is the maximum  $p_T$  and  $J_0$  is a modified Bessel function. There is one important  
 71 caveat, due to the square root, which converts from cross-section to amplitude. Because the square  
 72 root has two roots, one positive and one negative, one must flip the sign of  $\sqrt{d\sigma_c/dt}$  at each  
 73 diffractive minimum in  $d\sigma_c/dt$ .

74 This relationship is exact for  $t_{\max} = \infty$ . Unfortunately, this is not experimentally accessible.  
 75 The imposition of a finite  $t_{\max}$  can introduce artifacts into  $F(b)$ . In signal-processing language,  
 76 this is equivalent to the application of a square-pulse windowing function [10]. The output  $F(b)$   
 77 is the product of the Fourier transform of the true nuclear shape with the Fourier transform of  
 78 the windowing function. There are techniques to moderate these artifacts by using a different  
 79 windowing function, but they are problematic here because the window can only include 2-3 cycles  
 80 (one cycle between each diffractive minimum). So, we will not do this. Instead, we will make  
 81 transforms with different  $t_{\max}$  and compare the results from the three mass bins, for the same



**Figure 3:** Fourier transform  $F(b)$  for the three different mass bins, with (left)  $t_{\max} = 0.006 \text{ GeV}^2$  and (right)  $t_{\max} = 0.009 \text{ GeV}^2$

82  $t_{\max}$ . We use as a baseline  $t_{\max} = 0.006 \text{ GeV}^2$ , which gives results compatible with the previous  
 83 STAR photoproduction paper. It also avoids any of the sign flips due to the diffractive minima.  
 84 Figure 3 (left) shows  $F(b)$  for the three mass ranges with this baseline. The medium and high mass  
 85 curves are similar, showing a peak and a smooth fall-off, while the low-mass curve is noticeably  
 86 broader, with a flatter top. This is expected if saturation is present; the profile will broaden, since  
 87 absorption in the center cannot increase above one; in the black disk limit,  $F(b)$  would be constant,  
 88 with a sharp fall-off near the nuclear edges.  $F(b)$  drops below zero at large  $|b|$ ; this is likely due to  
 89 photoproduction in the opposing nucleus. Because of the parity inversion going from one nuclear  
 90 target to the other, this inversion introduces a negative sign [11].

91 Figure 3 (right) shows the effects of changing  $t_{\max}$  from 0.006 to 0.009  $\text{GeV}^2$  for the three  
 92 mass ranges. The medium and high mass ranges do not change much, but the low-mass  $F(b)$   
 93 grows considerably broader. This 'double-hump' behavior is also seen in the original STAR data  
 94 when  $t_{\max}$  is increased [5]. We also studied a smaller  $t_{\max}$ , 0.005  $\text{GeV}^2$ ; it had a similar  $F(b)$  to the  
 95 baseline.

### 96 3.1 STARlight as a null experiment

97 To understand the changes in  $F(b)$  with  $t_{\max}$ , we apply a similar procedure to simulated dipion  
 98 data from STARlight [12]. STARlight uses a Glauber calculation to determine the cross-section, but  
 99 it generates the  $p_T$  from the photon-nucleus scattering using a simple model for gold nuclei, with  
 100 the density following a Woods-Saxon distribution [13]. The photon  $p_T$  are generated following  
 101 the equivalent photon approximation [14], including the interference between dipion production  
 102 on the two nuclei [15]. So, STARlight simulates the non-scattering aspects of the reaction that  
 103 can affect  $p_T$ . Five million STARlight  $\rho^0 + \text{direct } \pi\pi$  were generated within the kinematic range  
 104  $|y| < 1$ ,  $|\eta_\pi| < 1$  and  $p_{T,\pi} > 100 \text{ MeV}/c$ , and divided up by mass range. The  $p_T$  spectra are  
 105 indistinguishable, and the resulting  $T(b)$  for all three mass bins look similar to the high-mass data.  
 106 When  $t_{\max}$  is varied, it also tends to follow the high-mass data.

#### 107 4. Conclusions and future work

108 The diffractive minima in  $d\sigma_c/dt$  show variation in depth with dipion mass. The Fourier  
 109 transform of  $d\sigma_c/dt$ ,  $F(b)$  also show apparent changes with pair mass. In the lowest mass bin,  $F(b)$   
 110 is flattened, consistent with the expectations from shadowing. The transform is closer to a black  
 111 disk than the other profiles, which are closer to the Woods-Saxon distribution that is implemented  
 112 in STARlight.

113 It is a pleasure to acknowledge useful conversations with Markus Diehl and Thomas Ullrich.  
 114 This work was funded by the U.S. DOE under contract number DE-AC-76SF0009.

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