

Formation of superheavy nuclei in cold fusion reactions

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Abstract

Within the concept of the dinuclear system (DNS), a dynamical model is proposed for describing the formation of superheavy nuclei in complete fusion reactions by incorporating the coupling of the relative motion to the nucleon transfer process. The capture of two heavy colliding nuclei, the formation of the compound nucleus and the de-excitation process are calculated by using an empirical coupled channel model, solving a master equation numerically and applying statistical theory, respectively. Evaporation residue excitation functions in cold fusion reactions are investigated systematically and compared with available experimental data. Maximal production cross sections of superheavy nuclei in cold fusion reactions with stable neutron-rich projectiles are obtained. Isotopic trends in the production of the superheavy elements $Z=110, 112, 114, 116, 118$ and 120 are analyzed systematically. Optimal combinations and the corresponding excitation energies are proposed.

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1 INTRODUCTION

The synthesis of very heavy (superheavy) nuclei is a very important subject in nuclear physics motivated with respect to the island of stability which is predicted theoretically, and has obtained much experimental progress with fusion-evaporation reactions [1, 2]. The existence of the superheavy nucleus (SHN) ($Z \geq 106$) is due to a strong binding shell effect against the large Coulomb repulsion. However, the shell effect will be reduced with increasing excitation energy

of the formed compound nucleus. Combinations with a doubly magic nucleus or nearly magic nucleus are usually chosen due to the larger reaction Q values. Reactions with ^{208}Pb or ^{209}Bi targets are proposed firstly by Yu. Ts. Oganessian et al. to synthesize SHN [3]. Six new elements with $Z=107-112$ were synthesized in cold fusion reactions for the first time and investigated at GSI (Darmstadt, Germany) with the heavy-ion accelerator UNILAC and the separator SHIP [1, 4]. Recently, experiments on the synthesis of element 113 in the $^{70}\text{Zn} + ^{209}\text{Bi}$ reaction have been performed successfully at RIKEN (Tokyo, Japan) [5]. Superheavy elements $Z=113-116, 118$ were synthesized at FLNR in Dubna (Russia) with double magic nucleus ^{48}Ca bombarding actinide nuclei [6]. Reasonable understanding on the formation of SHN in massive fusion reactions is still a challenge for theory.

In accordance with the evolution of two heavy colliding nuclei, the whole process of the compound nucleus formation and decay is usually divided into three reaction stages, namely the capture process of the colliding system to overcome Coulomb barrier, the formation of the compound nucleus to pass over the inner fusion barrier as well as the de-excitation of the excited compound nucleus against fission. The transmission in the capture process depends on the incident energy and relative angular momentum of the colliding nuclei, and is the same as in the fusion of light and medium mass systems. The complete fusion of the heavy system after capture in competition with quasi-fission is very important in the estimation of the SHN production. At present it is still difficult to make an accurate description of the fusion dynamics. After the capture and the subsequent evolution to form the compound nucleus, the thermal compound nucleus will decay by the emission of light particles and γ -rays against fission. The above three stages will affect the formation of evaporation residues observed in laboratories. The evolution of the whole process of massive heavy-ion collisions is very complicated at near barrier energies. Most of theoretical approaches on the formation of SHN have a similar viewpoint in the description of the capture and the de-excitation stages, but there is no consensus on the compound nucleus formation process. There are mainly two sorts of models, whether the compound nucleus is formed along the radial variable (internuclear distance) or by nucleon transfer at the minimum position of the interaction potential after capture of the colliding system. Several transport models have been established to understand the fusion mechanism of two heavy colliding nuclei leading to SHN formation, such as the macroscopic dynamical model [7, 8], the fluctuation-dissipation model [9], the concept of nucleon collectivization [10] and the dinuclear system model [11]. With these models experimental data can be reproduced and some new results have been predicted. The models differ from each other, and sometimes contradictory physical ideas are used.

Further improvements on the mentioned models have to be made. Here we use an improved dinuclear system model (DNS), in which the nucleon transfer is coupled with the relative motion and the barrier distribution of the colliding system is included. We present a new and extended investigation of the production of superheavy nuclei in lead-based cold fusion reactions. For that we make use of a formalism describing the nucleon transfer with a set of microscopically derived master equations.

In Sec. 2 we give a description on the DNS model. Calculated results of fusion dynamics and SHN production in cold fusion reactions are given in Sec. 3. In Sec. 4 conclusions are discussed.

2 DINUCLEAR SYSTEM MODEL

The dinuclear system (DNS) is a molecular configuration of two touching nuclei which keep their own individuality [11]. Such a system has an evolution along two main degrees of freedom: (i) the relative motion of the nuclei in the interaction potential to form the DNS and the decay of the DNS (quasi-fission process) along the R degree of freedom (internuclear motion), (ii) the transfer of nucleons in the mass asymmetry coordinate $\eta = (A_1 - A_2)/(A_1 + A_2)$ between two nuclei, which is a diffusion process of the excited systems leading to the compound nucleus formation. Off-diagonal diffusion in the surface (A_1, R) is not considered since we assume the DNS is formed at the minimum position of the interaction potential of two colliding nuclei. In this concept, the evaporation residue cross section is expressed as a sum over partial waves with angular momentum J at the centre-of-mass energy $E_{c.m.}$,

$$\sigma_{ER}(E_{c.m.}) = \frac{\pi \hbar^2}{2\mu E_{c.m.}} \sum_{J=0}^{J_{max}} (2J+1) T(E_{c.m.}, J) P_{CN}(E_{c.m.}, J) W_{sur}(E_{c.m.}, J). \quad (1)$$

Here, $T(E_{c.m.}, J)$ is the transmission probability of the two colliding nuclei overcoming the Coulomb potential barrier in the entrance channel to form the DNS. In the same manner as in the nucleon collectivization model [10], the transmission probability T is calculated by using the empirical coupled channel model, which can reproduce very well available experimental capture cross sections [10, 12]. P_{CN} is the probability that the system will evolve from a touching configuration into the compound nucleus in competition with quasi-fission of the DNS and fission of the heavy fragment. The last term is the survival probability of the formed compound nucleus, which can be estimated with the statistical evaporation model by considering the competition between neutron evaporation and fission [12]. We take the maximal angular momentum as $J_{max} = 30$ since the fission barrier of the heavy nucleus disappears at high spin [13].

In order to describe the fusion dynamics as a diffusion process in mass asymmetry, the analytical solution of the Fokker-Planck equation [11] and the numerical solution of the master equation [14, 15] have been used, which were also used to treat deep inelastic heavy-ion collisions. Here, the fusion probability is obtained by solving a master equation numerically in the potential energy surface of the DNS. The time evolution of the distribution function $P(A_1, E_1, t)$ for fragment 1 with mass number A_1 and excitation energy E_1 is described by the following master equation [16, 17],

$$\frac{dP(A_1, E_1, t)}{dt} = \sum_{A'_1} W_{A_1, A'_1}(t) \left[d_{A_1} P(A'_1, E'_1, t) - d_{A'_1} P(A_1, E_1, t) \right] - \left[\Lambda^{qf}(\Theta(t)) + \Lambda^{fis}(\Theta(t)) \right] P(A_1, E_1, t). \quad (2)$$

Here W_{A_1, A'_1} is the mean transition probability from the channel (A_1, E_1) to (A'_1, E'_1) , while d_{A_1} denotes the microscopic dimension corresponding to the macroscopic state (A_1, E_1) . The sum is taken over all possible mass numbers that fragment A'_1 may take (from 0 to $A = A_1 + A_2$), but only one nucleon transfer is considered in the model with $A'_1 = A_1 \pm 1$. The excitation energy E_1 is the local excitation energy ε_1^* with respect to fragment A_1 , which is determined by the dissipation energy from the relative motion and the potential energy of the corresponding DNS and will be shown later in Eqs.(8-9). The dissipation energy is described by the parametrization method of the classical deflection function [18, 19]. The motion of nucleons in the interacting potential is governed by the single-particle Hamiltonian [12, 14]:

$$H(t) = H_0(t) + V(t) \quad (3)$$

with

$$\begin{aligned} H_0(t) &= \sum_K \sum_{\nu_K} \varepsilon_{\nu_K}(t) a_{\nu_K}^\dagger(t) a_{\nu_K}(t), \\ V(t) &= \sum_{K, K'} \sum_{\alpha_K, \beta_{K'}} u_{\alpha_K, \beta_{K'}}(t) a_{\alpha_K}^\dagger(t) a_{\beta_{K'}}(t) = \sum_{K, K'} V_{K, K'}(t). \end{aligned} \quad (4)$$

Here the indices K, K' ($K, K' = 1, 2$) denote the fragments 1 and 2. The quantities ε_{ν_K} and $u_{\alpha_K, \beta_{K'}}$ represent the single particle energies and the interaction matrix elements, respectively. The single particle states are defined with respect to the centers of the interacting nuclei and are assumed to be orthogonalized in the overlap region. So the annihilation and creation operators are dependent on time. The single particle matrix elements are parameterized by

$$u_{\alpha_K, \beta_{K'}}(t) = U_{K, K'}(t) \left\{ \exp \left[-\frac{1}{2} \left(\frac{\varepsilon_{\alpha_K}(t) - \varepsilon_{\beta_{K'}}(t)}{\Delta_{K, K'}(t)} \right)^2 \right] - \delta_{\alpha_K, \beta_{K'}} \right\}, \quad (5)$$

which contains some parameters $U_{K,K'}(t)$ and $\Delta_{K,K'}(t)$. The detailed calculation of these parameters and the mean transition probabilities were described in Refs. [14, 12].

The evolution of the DNS along the variable R leads to the quasi-fission of the DNS. The quasi-fission rate Λ^{qf} can be estimated with the one dimensional Kramers formula [20, 21]:

$$\Lambda^{qf}(\Theta(t)) = \frac{\omega}{2\pi\omega^{B_{qf}}} \left(\sqrt{\left(\frac{\Gamma}{2\hbar}\right)^2 + (\omega^{B_{qf}})^2} - \frac{\Gamma}{2\hbar} \right) \exp\left(-\frac{B_{qf}(A_1, A_2)}{\Theta(t)}\right). \quad (6)$$

Here the quasi-fission barrier measures the depth of the pocket of the interaction potential. The local temperature is given by the Fermi-gas expression $\Theta = \sqrt{\varepsilon^*/a}$ corresponding to the local excitation energy ε^* and level density parameter $a = A/12 \text{ MeV}^{-1}$. $\omega^{B_{qf}}$ is the frequency of the inverted harmonic oscillator approximating the interaction potential of two nuclei in R around the top of the quasi-fission barrier, and ω is the frequency of the harmonic oscillator approximating the potential in R at the bottom of the pocket. The quantity Γ denotes the double average width of the contributing single-particle states, which determines the friction coefficients: $\gamma_{ii'} = \frac{\Gamma}{\hbar}\mu_{ii'}$, with $\mu_{ii'}$ being the inertia tensor. Here we use constant values $\Gamma = 2.8 \text{ MeV}$, $\hbar\omega^{B_{qf}} = 2.0 \text{ MeV}$ and $\hbar\omega = 3.0 \text{ MeV}$ for the following reactions. The Kramers formula is derived at the quasi-stationary condition of the temperature $\Theta(t) < B_{qf}(A_1, A_2)$. However, the numerical calculation in Ref. [21] indicated that Eq.(6) is also available at the condition of $\Theta(t) > B_{qf}(A_1, A_2)$. In the reactions of synthesizing SHN, there is the possibility of the fission of the heavy fragment in the DNS. Since the fissility increases with the charge number of the nucleus, the fission of the heavy fragment can affect the quasi-fission and fusion when the DNS evolves towards larger mass asymmetry. The fission rate Λ^{fis} can also be treated with the one-dimensional Kramers formula [20]

$$\Lambda^{fis}(\Theta(t)) = \frac{\omega_{g.s.}}{2\pi\omega_f} \left(\sqrt{\left(\frac{\Gamma_0}{2\hbar}\right)^2 + \omega_f^2} - \frac{\Gamma_0}{2\hbar} \right) \exp\left(-\frac{B_f(A_1, A_2)}{\Theta(t)}\right), \quad (7)$$

where $\omega_{g.s.}$ and ω_f are the frequencies of the oscillators approximating the fission-path potential at the ground state and on the top of the fission barrier for nucleus A_1 or A_2 (larger fragment), respectively. Here, we take $\hbar\omega_{g.s.} = \hbar\omega_f = 1.0 \text{ MeV}$, $\Gamma_0 = 2 \text{ MeV}$. The fission barrier is calculated as a sum of a macroscopic part and the shell correction used in Refs. [22]. The fission of the heavy fragment is not in favor of the diffusion of the system to light fragment distribution. Therefore, it leads to a slightly decrease of the fusion probability (seeing Eq.(17)).

In the relaxation process of the relative motion, the DNS will be excited due to the dissipation of the relative kinetic energy. The excited system opens a valence space $\Delta\varepsilon_K$ in fragment K ($K = 1, 2$), which has a symmetrical distribution around the Fermi surface. Only the particles in the

states within the valence space are actively involved in excitation and transfer. The averages on these quantities are performed in the valence space:

$$\Delta\varepsilon_K = \sqrt{\frac{4\varepsilon_K^*}{g_K}}, \varepsilon_K^* = \varepsilon^* \frac{A_K}{A}, g_K = \frac{A_K}{12} \quad (8)$$

where ε^* is the local excitation energy of the DNS, which provides the excitation energy for the mean transition probability. There are $N_K = g_K \Delta\varepsilon_K$ valence states and $m_K = N_K/2$ valence nucleons in the valence space $\Delta\varepsilon_K$, which give the dimension $d(m_1, m_2) = \binom{N_1}{m_1} \binom{N_2}{m_2}$. The local excitation energy is defined as

$$\varepsilon^* = E_x - (U(A_1, A_2) - U(A_P, A_T)). \quad (9)$$

Here $U(A_1, A_2)$ and $U(A_P, A_T)$ are the driving potentials of fragments A_1, A_2 and fragments A_P, A_T (at the entrance point of the DNS), respectively. The excitation energy E_x of the composite system is converted from the relative kinetic energy loss, which is related to the Coulomb barrier B [23] and determined for each initial relative angular momentum J by the parametrization method of the classical deflection function [18, 19]. So E_x is coupled with the relative angular momentum.

The potential energy surface (PES, i.e. the driving potential) of the DNS is given by

$$U(A_1, A_2, J, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) = B(A_1) + B(A_2) - [B(A) + V_{rot}^{CN}(J)] + V(A_1, A_2, J, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) \quad (10)$$

with $A_1 + A_2 = A$. Here $B(A_i)$ ($i = 1, 2$) and $B(A)$ are the negative binding energies of the fragment A_i and the compound nucleus A , respectively, in which the shell and the pairing corrections are included reasonably. V_{rot}^{CN} is the rotation energy of the compound nucleus. β_i represent quadrupole deformations of the two fragments. θ_i denote the angles between the collision orientations and the symmetry axes of deformed nuclei. The interaction potential between fragment 1 (Z_1, A_1) and 2 (Z_2, A_2) includes the nuclear, Coulomb and centrifugal parts as

$$V(A_1, A_2, J, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) = V_N(A_1, A_2, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) + V_C(A_1, A_2, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) + \frac{J(J+1)\hbar^2}{2\mu\mathbf{R}^2}, \quad (11)$$

where the reduced mass is given by $\mu = m \cdot A_1 A_2 / A$ with the nucleon mass m . The nuclear potential is calculated using the double-folding method based on Skyrme interaction force without considering the momentum and the spin dependence as [24]

$$V_N = C_0 \left\{ \frac{F_{in} - F_{ex}}{\rho_0} \left[\int \rho_1^2(\mathbf{r}) \rho_2(\mathbf{r} - \mathbf{R}) d\mathbf{r} + \int \rho_1(\mathbf{r}) \rho_2^2(\mathbf{r} - \mathbf{R}) d\mathbf{r} \right] + F_{ex} \int \rho_1(\mathbf{r}) \rho_2(\mathbf{r} - \mathbf{R}) d\mathbf{r} \right\}, \quad (12)$$

with

$$F_{in,ex} = f_{in,ex} + f'_{in,ex} \frac{N_1 - Z_1}{A_1} \frac{N_2 - Z_2}{A_2}, \quad (13)$$

which is dependent on the nuclear densities and on the orientations of deformed nuclei in the collision [25]. The parameters $C_0 = 300 \text{ MeV} \cdot \text{fm}^3$, $f_{in} = 0.09$, $f_{ex} = -2.59$, $f'_{in} = 0.42$, $f'_{ex} = 0.54$, $\rho_0 = 0.16 \text{ fm}^{-3}$ are used in the calculation. The Woods-Saxon density distributions are expressed for two nuclei as

$$\rho_1(\mathbf{r}) = \frac{\rho_0}{1 + \exp[(\mathbf{r} - \mathfrak{R}_1(\theta_1))/a_1]}, \quad (14)$$

and

$$\rho_2(\mathbf{r} - \mathbf{R}) = \frac{\rho_0}{1 + \exp[(|\mathbf{r} - \mathbf{R}| - \mathfrak{R}_2(\theta_2))/a_2]}. \quad (15)$$

Here $\mathfrak{R}_i(\theta_i)$ ($i = 1, 2$) are the surface radii of the nuclei with $\mathfrak{R}_i(\theta_i) = R_i(1 + \beta_i Y_{20}(\theta_i))$, and the spheroidal radii R_i . The parameters a_i represent the surface diffusion coefficients, which are taken 0.55 fm in the calculation. The Coulomb potential is obtained by Wong's formula [26], which agrees well with the double-folding procedure. In the actual calculation, the distance \mathbf{R} between the centers of the two fragments is chosen to be the value which gives the minimum of the interaction potential, in which the DNS is considered to be formed. So the PES depends only on the mass asymmetry degree of freedom η , which gives the driving potential of the DNS as shown in Fig.1 for the reaction $^{70}\text{Zn} + ^{208}\text{Pb}$ at the tip-tip, the belly-belly and at the fixed $(0^\circ, 0^\circ)$ and $(90^\circ, 90^\circ)$ orientations. Here, we should note that the tip-tip orientation is different with $(0^\circ, 0^\circ)$. We rotate $\frac{\pi}{2}$ for the fragment with negative quadrupole deformation. However, the orientation angle θ_i is fixed for all fragments. The same procedure is taken for the belly-belly and $(90^\circ, 90^\circ)$. The Businaro-Gallone (B.G.) point marks the maximum position of the driving potential on the left side of the initial combination η_i . Some averaging over all orientations should be carried out in the nucleon transfer process. However, the tip-tip orientation which gives the minimum of the PES is in favor of nucleon transfer and is chosen in the calculation. For the reaction $^{70}\text{Zn} + ^{208}\text{Pb}$, the tip-tip orientation ($B_{fus}=20.98$ MeV) has lower inner fusion barrier than the belly-belly orientation ($B_{fus}=25.71$ MeV). However, the belly-belly orientation appears an obvious hump towards symmetric combinations (reducing $|\eta_i|$), which is in favor of the compound nucleus formation against the quasi-fission. Both of the two factors may affect the values of P_{CN} (seeing Eq.(17)). In Fig.2 we show the comparison of the formation probability of the compound nucleus in the reaction $^{70}\text{Zn} + ^{208}\text{Pb}$ as functions of angular momenta ($E_{c.m.}=254.08$ MeV, $E_{CN}^*=12$ MeV) and incident c.m. energies ($J=0$) at the tip-tip and the belly-belly orientations, respectively. The

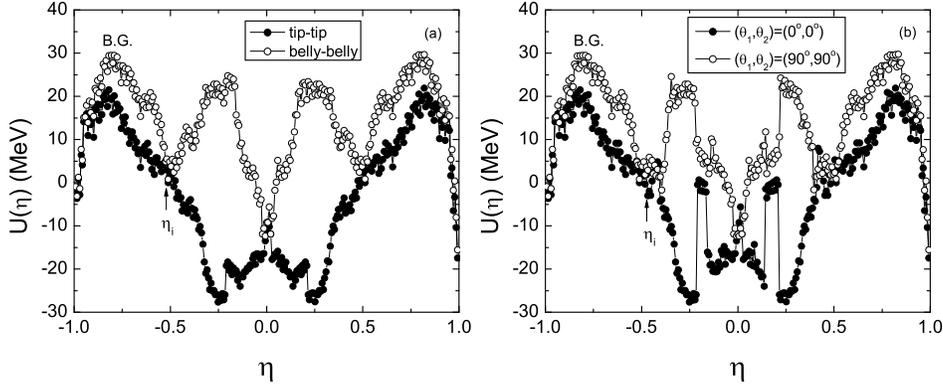


Figure 1: The driving potential of the DNS for the reaction $^{70}\text{Zn} + ^{208}\text{Pb}$ as a function of the mass asymmetry η at the different orientations.

effects of the collision orientations on the fusion cross section were also studied in detail by A. Nasirov et al. [27] for deformed combination systems.

After reaching the time of reaction in the evolution of $P(A_1, E_1, t)$, all those components on the left side of the B.G. point as shown in Fig.1 (a) contribute to the compound nucleus formation. The hindrance in the diffusion process by nucleon transfer to form the compound nucleus is the inner fusion barrier B_{fus} , which is defined as the difference of the driving potential at the B.G. point and at the entrance position. Nucleon transfer to more symmetric fragments will be in favor of quasi-fission. The formation probability of the compound nucleus at Coulomb barrier B (here the barrier distribution $f(B)$ is considered) and angular momentum J is given by

$$P_{CN}(E_{c.m.}, J, B) = \sum_{A_1=1}^{A_{BG}} P(A_1, E_1, \tau_{int}(E_{c.m.}, J, B)). \quad (16)$$

Here the interaction time $\tau_{int}(E_{c.m.}, J, B)$ is obtained using the deflection function method [28]. We obtain the fusion probability as

$$P_{CN}(E_{c.m.}, J) = \int f(B) P_{CN}(E_{c.m.}, J, B) dB, \quad (17)$$

where the barrier distribution function is taken in asymmetric Gaussian form [10, 12]. So the fusion cross section is written as

$$\sigma_{fus}(E_{c.m.}) = \frac{\pi \hbar^2}{2\mu E_{c.m.}} \sum_{J=0}^{\infty} (2J+1) T(E_{c.m.}, J) P_{CN}(E_{c.m.}, J). \quad (18)$$

The survival probability of the excited compound nucleus in the cooling process by means of

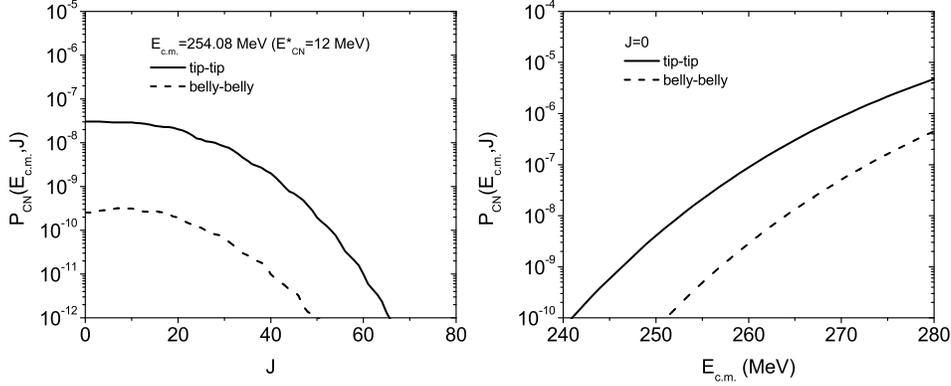


Figure 2: Dependence of the fusion probability on angular momenta and incident c.m. energies in the reaction $^{70}\text{Zn} + ^{208}\text{Pb}$ at the tip-tip and the belly-belly orientations, respectively.

the neutron evaporation in competition with fission is expressed as following:

$$W_{sur}(E_{CN}^*, x, J) = P(E_{CN}^*, x, J) \prod_{i=1}^x \left(\frac{\Gamma_n(E_i^*, J)}{\Gamma_n(E_i^*, J) + \Gamma_f(E_i^*, J)} \right)_i, \quad (19)$$

where the E_{CN}^*, J are the excitation energy and the spin of the compound nucleus, respectively. E_i^* is the excitation energy before evaporating the i th neutron, which has the relation:

$$E_{i+1}^* = E_i^* - B_i^n - 2T_i, \quad (20)$$

with the initial condition $E_1^* = E_{CN}^*$. B_i^n is the separation energy of the i th neutron. The nuclear temperature T_i is given by $E_i^* = aT_i^2 - T_i$ with the level density parameter a . $P(E_{CN}^*, x, J)$ is the realization probability of emitting x neutrons. The widths of neutron evaporation and fission are calculated using the statistical model. The details can be found in Ref. [12].

3 RESULTS AND DISCUSSION

3.1 Evaporation residue cross sections

The evaporation residues observed in laboratories by the consecutive α decay are mainly produced by the complete fusion reactions, in which the fusion dynamics and the structure properties of the compound nucleus affects their production. Within the framework of the DNS model, we calculated the evaporation residue cross sections producing SHN $Z=110-113$ in cold fusion reactions as shown in Fig.3, and compared them with GSI data for 110-112 [1] and RIKEN results [5] for

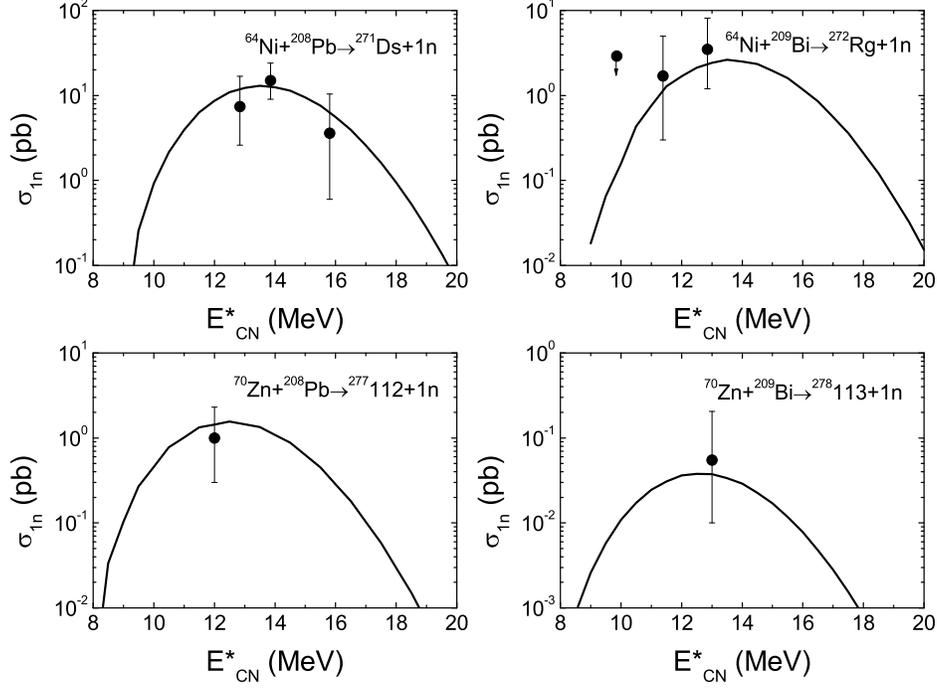


Figure 3: Comparison of the calculated evaporation residue excitation functions and the experimental data to synthesize superheavy elements $Z=110-113$ in cold fusion reactions.

113. The excitation energy is obtained by $E_{CN}^* = E_{c.m.} + Q$, where $E_{c.m.}$ is the incident energy in the center-of-mass system. The Q value is given by $Q = \Delta M_P + \Delta M_T - \Delta M_C$, and the corresponding mass defects are taken from Ref.[29] for projectile, target and compound nucleus, respectively. Usually, neutron-rich projectiles are used to synthesize SHN experimentally, such as ^{64}Ni and ^{70}Zn , which can enhance the survival probability W_{sur} in Eq.(1) of the formed compound nucleus due to smaller neutron separation energy. The maximal production cross sections from Ds to 113 are reduced rapidly because the inner fusion barrier is increasing. Within error bars the experimental results can be reproduced very well. There is no other adjustable parameters in the calculation. Within the same scheme, we analyzed the evaporation residue excitation functions with projectiles ^{73}Ge , ^{82}Se , ^{86}Kr and ^{88}Sr to produce superheavy elements $Z=114, 116, 118, 120$ in Fig.4. An upper-limit for the cross section producing 118 was obtained in Berkeley [30].

In Fig.5 we show the comparison of the calculated maximal production cross sections of superheavy elements $Z=102-120$ in cold fusion reactions by evaporating one neutron with experimental data [1, 4]. The production cross sections decrease rapidly with increasing the charge number of the synthesized compound nucleus, such as from $0.2 \mu\text{b}$ for the reaction $^{48}\text{Ca} + ^{208}\text{Pb}$ to 1 pb

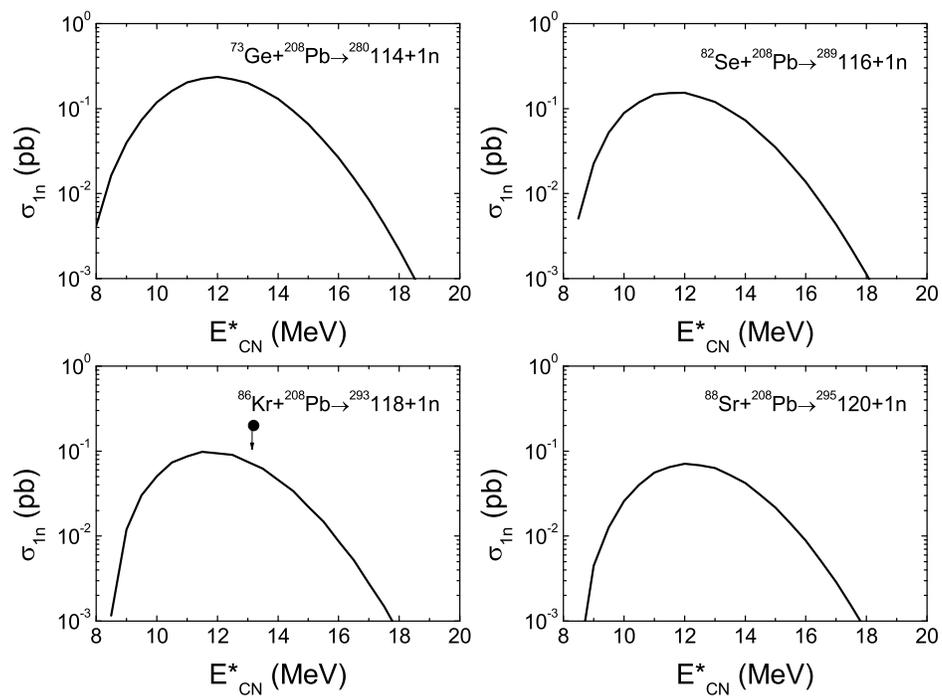


Figure 4: The same as in Fig.3, but for projectiles ^{73}Ge , ^{82}Se , ^{86}Kr and ^{88}Sr in cold fusion reactions to produce superheavy elements $Z=114$, 116, 118, 120.

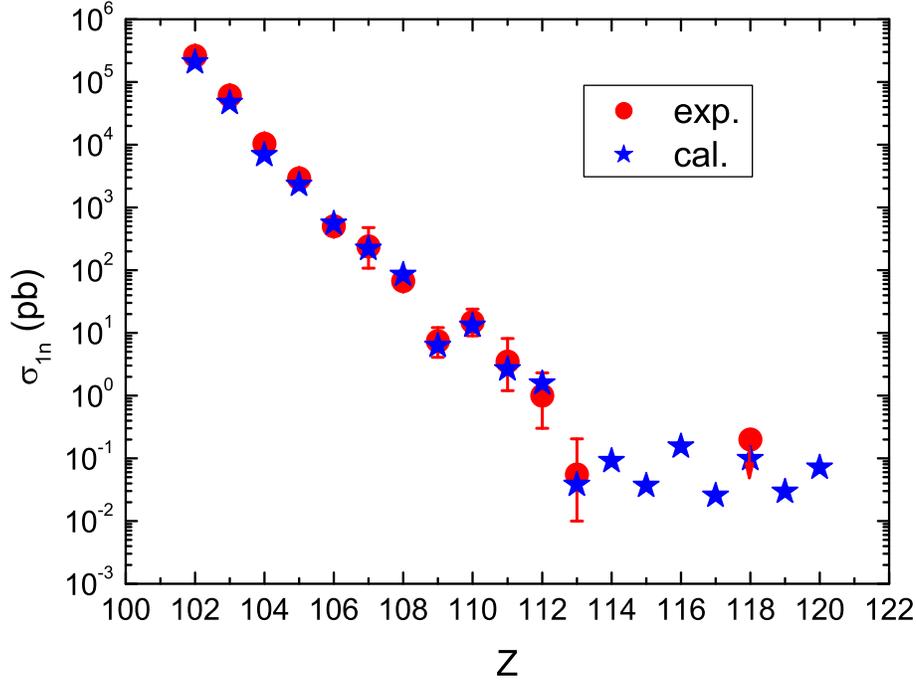


Figure 5: (Color online) Maximal production cross sections of superheavy elements $Z=102-120$ in cold fusion reactions based ^{208}Pb and ^{209}Bi targets with projectile nuclei ^{48}Ca , ^{50}Ti , ^{54}Cr , ^{58}Fe , ^{64}Ni , ^{70}Zn , ^{76}Ge , ^{82}Se , ^{86}Kr and ^{88}Sr , and compared with experimental data.

for $^{70}\text{Zn} + ^{208}\text{Pb}$, and around even below 0.1 pb for synthesizing $Z \geq 113$. It seems to be difficult to synthesize superheavy elements $Z \geq 113$ in cold fusion reactions at the present facilities. The calculated results are in good agreement with the experimental data. In the DNS concept, the inner fusion barrier increases with reducing mass asymmetry, which leads to a decrease of the formation probability of the compound nucleus as shown in Fig.6. On the other hand, the quasi-fission and the fission of the heavy fragments in the nuclear transfer process become more and more important if the mass asymmetry ($|\eta_i|$) of the projectile-target combination is decreasing, which also reduce the formation probability. There appears a little increase for $Z \geq 118$, which is related to the decreased inner fusion barriers of the three systems. The survival of the thermal compound nucleus in the fusion reactions are mainly affected by the neutron evaporation energy, the fission barrier and the level density. The survival probability has strong structure effects as shown in Fig.6. Accurate calculation of the survival probability is very necessary to obtain reasonable evaporation residue cross sections.

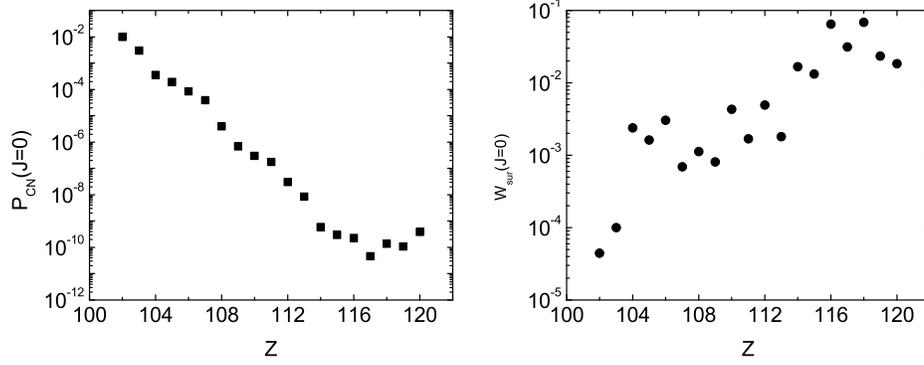


Figure 6: The fusion and the survival probabilities at $J=0$ as functions of the charge numbers of the compound nuclei with the same combinations as stated in the caption of Fig.5.

3.2 Isotopic dependence of the production cross sections

The production of the SHN depends on the isotopic combination of the target and projectile in the cold fusion reactions. For example, the maximal cross section is $3.5 \pm_{1.8}^{2.7}$ pb for the reaction $^{62}Ni + ^{208}Pb \rightarrow ^{269}Ds + 1n$, however $15 \pm_6^9$ pb for the reaction $^{64}Ni + ^{208}Pb \rightarrow ^{271}Ds + 1n$ [1, 31]. Further investigations on the isotopic trends are very necessary for predicting the optimal combinations and the optimal excitation energies (incident energies) to synthesize SHN. In Fig.7 we show the calculated isotopic trends in producing superheavy elements $Z=110, 112$ for the reactions $^ANi + ^{208}Pb$ and $^AZn + ^{208}Pb$ (squares with lines), and compare them with the results of G.G. Adamian et al. [32] (diamonds and triangles) and the available experimental data [1] (circles with error bars). We find that the isotopes $^{63,64,65}Ni$ and $^{67,70}Zn$ are suitable to synthesize superheavy elements 110 and 112, respectively. The isotopes ^{64}Ni and ^{67}Zn have larger production cross section, which is consistent with the results of G.G. Adamian et al. But for other isotopes, the two methods give slightly different results. For example, our model gives that ^{70}Zn has larger cross section to produce elements 110 than the isotope ^{68}Zn . However, the opposite trend is obtained by G.G. Adamian et al. Therefore, it need more accurate description on the three stages of the formation of SHN. Further experimental data is also required to examine the theoretical models. In the DNS model, the isotopic trends are mainly determined by both the fusion and survival probabilities. Of course, the transmission probability of two colliding nuclei can also affect the trends since the initial quadrupole deformations depend on the isotopes. When the neutron number of the projectile is increasing, the DNS gets more symmetrical and the fusion probability

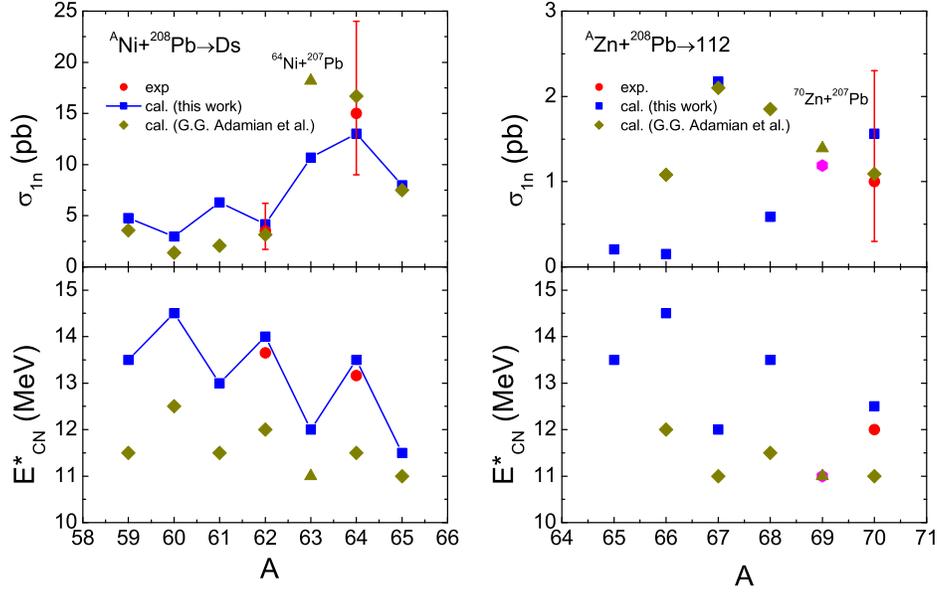


Figure 7: (Color online) Isotopic dependence of the calculated maximal production cross sections and the corresponding excitation energies in the synthesis of superheavy elements $Z=110, 112$ for the reactions $^A Ni + ^{208} Pb$ and $^A Zn + ^{208} Pb$, and compared with the results of G.G. Adamian et al. [32] and the experimental data [1, 4].

decreases if the DNS does not consist of more stable nuclei due to a higher inner fusion barrier. A smaller neutron separation energy and a larger shell correction lead to a larger survival probability. The compound nucleus with closed neutron shells has larger shell correction energy and neutron separation energy. With the same procedure, we analyzed the dependence of the production cross sections on the isotopes Ge and Se to produce the superheavy elements $Z=114, 116$ shown in Fig.8 as well as on the isotopes Kr and Sr to synthesize the superheavy elements $Z=114, 116$ with a $^{208} Pb$ target as shown in Fig.9. It results that the projectiles $^{73} Ge$, $^{79} Se$, $^{85} Kr$ and $^{87,88} Sr$ are favorable to synthesize the new superheavy elements $Z=114, 116, 118$ and 120 . The corresponding excitation energies are also given in the figures. The compound nuclei with neutron-rich isotopes $^{76} Ge$, $^{80,82} Se$ and $^{84,86} Kr$ are near the sub-closure at $N=172$. These compound nuclei have larger one-neutron separation energies, and the initial combinations smaller mass asymmetries leading to smaller evaporation residue cross sections.

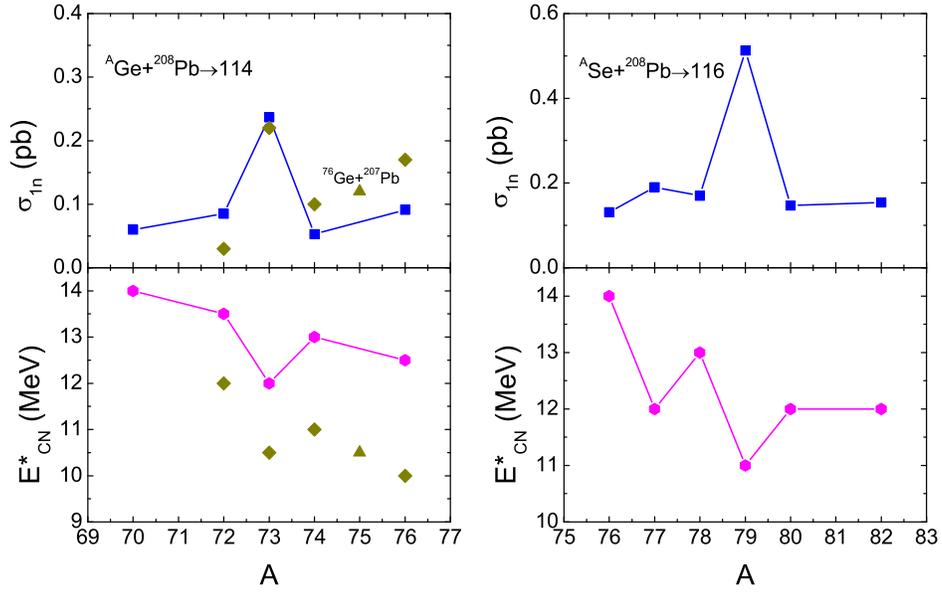


Figure 8: (Color online) The same as in Fig. 7, but for isotopes Ge and Se to produce superheavy elements $Z=114, 116$.

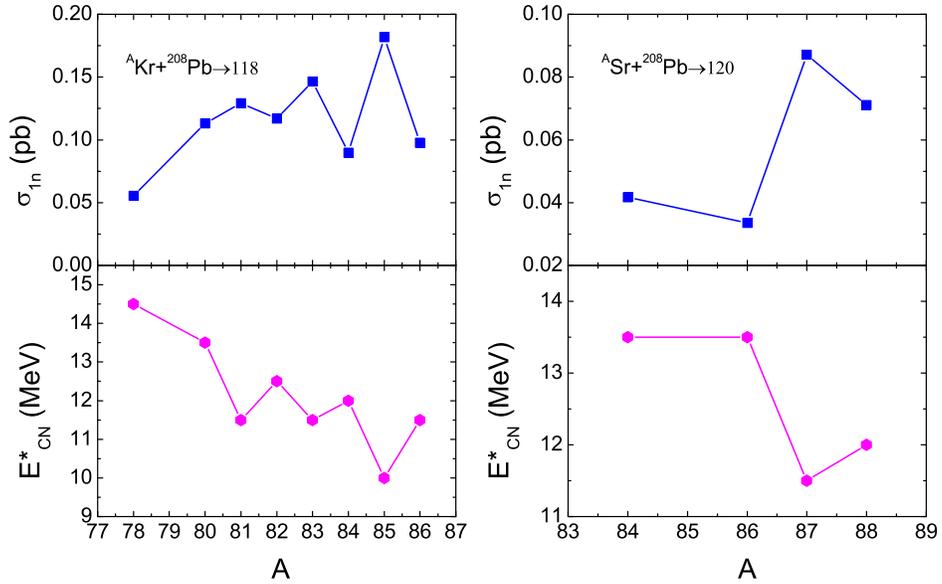


Figure 9: (Color online) The same as in Fig. 7, but for isotopes Kr and Sr based ^{208}Pb target.

4 CONCLUSIONS

Within the DNS concept, a dynamical model is worked out for describing the production of superheavy residues in the fusion-evaporation reactions, in which the formation of the superheavy compound nucleus is described by a master equation which is solved numerically and includes the quasi-fission of the DNS and the fission of the heavy fragments in the nucleon transfer process. By using the DNS model, the fusion dynamics and the evaporation residue excitation functions in cold fusion reactions are investigated systematically. The calculated results are in good agreement with available experimental data within error bars. Isotopic trends in the production of superheavy elements are analyzed systematically. It is shown that the isotopes $^{63,64,65}\text{Ni}$, $^{67,70}\text{Zn}$, ^{73}Ge , ^{79}Se , ^{85}Kr and $^{87,88}\text{Sr}$ are favorable to produce the superheavy elements $Z=110, 112, 114, 116, 118$ and 120 at the stated excitation energies.

The physical nature of the synthesis of heavy fissile nuclei in massive fusion reactions is very complicated, which involves not only certain quantities which crucially influence the whole process, but also the dynamics of the process is important. The coupling of the dynamic deformation and the nucleon transfer in the course of overcoming the multi-dimensional PES has to be considered in the DNS model. The height of the fission barrier for the heavy or superheavy nuclei should be more studied, which is mainly determined by the shell correction energies at the ground state and at the saddle point [33]. It plays an very important role in the calculation of the survival probability. Further work is in progress.

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