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Mantle upwellings

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above slab graveyards linked to the global geoid lows

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SUPPLEMENTARY MATERIAL

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Sonja Spasojevic¹, Michael Gurnis¹ and Rupert Sutherland²

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¹Seismological Laboratory, California Institute of Technology, Pasadena, CA 91125,

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USA

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²GNS Science, PO Box 30368, Lower Hutt 5040, New Zealand

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Supplementary Figure S1. Details of velocity structure for models S20RTS¹ (first column) and SB4L18² (second column), and model TX2005³ (third column) in the zones of geoid minima. (a) Integrated tomography in depth range 2050-2850 km; (b) Integrated tomography in depth range 300-1000 km; (c) Cross section from North America to Ross Sea; (d) Cross section from central Asia to Ross Sea; (e) Correlation coefficient between observed geoid and tomography calculated at every 100 km depth; (f) Observed geoid. Semi-transparent outlines on (a-b) cover zone of global geoid high; blue and red dashed lines (c-d) indicate lower mantle high velocity and upper-to-mid mantle low velocity anomalies of interest, respectively; black, blue and red lines on (e) show mean correlation coefficient between whole geoid, areas of negative geoid and areas of positive geoid, respectively; red lines on (f) indicate position of great circle cross-sections intersecting geoid low. Correlation coefficient between observed geoid and tomography models (e) is calculated as a product of values divided by product of standard deviations at every 100 km depth. The mean value of correlation coefficient is then calculated for whole geoid, areas of geoid lows, and geoid highs.

Integrated tomography plots (a-b) show a correlation between geoid low (f) and both seismically fast regions in lower mantle (a) and slow regions in upper-to-mid mantle (b) for all investigated tomography models. In the region of NE Pacific geoid low, all models define a seismically fast anomaly in the lower 500-1000 km of mantle (c), which is probably related to an ancient subducted slab that hasn't been recognized previously, except by analysis of SKS-SKKS splitting discrepancies⁴. A zone of upper-mid mantle seismically slow velocities is located above this fast anomaly (c), model SB4L18² defines

37 this structure largely in the lower mantle, while models S20RTS¹ and TX2005³ place it at
38 depths up to 800 km. In the Ross Sea region (c-d), all models show coherent upper-mid
39 mantle seismically slow region. Fast seismic anomaly in the lower mantle appears to
40 consist of several separate structures, possibly corresponding to different stages of
41 Gondwana subduction. In the zone of Indian Ocean geoid low, all models clearly define
42 fast seismic anomalies in the lower mantle (d), that was previously attributed to Mesozoic
43 Tethyan subduction⁵. In the upper-to-mid mantle, TX2005 defines the most coherent
44 slow region in depth range of 300-800 km (d) in the region of local geoid low (10°S to
45 10°N), while models S20RTS and SB4L18 show no particularly distinctive region of
46 slow velocities (d). Correlation analysis between observed geoid tomography and various
47 component of geoid (e) indicate that negative geoid is correlated with low velocity
48 tomographic anomalies in upper 1200-1500 km of mantle and high velocity seismic
49 anomalies in the lower mantle. Positive geoid is correlated with high velocity anomalies
50 in upper 800 km of mantle and negative seismic anomalies in the lower mantle.

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Supplementary Figure S2. Details of viscosity structure. (a) Tectonic regionalization map with high viscosity cratons, low viscosity mantle wedges and intermediate viscosity background regions; (b) S20RTS tomography at 250 km depth with outlines (green) of geologically defined cratons⁶; (c) Radial viscosity structure for models with tectonic regionalization; (d) Radial viscosity structure for models without tectonic regionalization; (e-f) Viscosity cross-sections for models with (e) and without (f) tectonic regionalization; (g) Global temperature cross-section; (h) Regional cross-section through NE Pacific geoid low with velocity vectors overlay. Position of cross-sections (e-h) is shown with black line on (a); red, green and blue rectangles on (c) show upper mantle range of viscosities for cratons, background and wedges, respectively; grey rectangles on (c-d) show range of viscosities in lower and upper mantle.

Following the experience from previous studies that use scaled tomographic models for geoid and gravity predictions to either define only the best fitting radial viscosity structure^{7,8,9,10,11}, without imposing any lateral tectonic viscosity parameterization, or models in which viscosity is not just a function of depth and temperature (seismic velocity), but also have pre-imposed large-scale variations based on upper mantle structure and tectonics^{12,13,14,15}, we develop two types of models: (1) models with tectonic regionalization in the upper mantle (a-c, e), and (2) models without tectonic regionalization in the upper mantle (d, f). For models with tectonic regionalization, high viscosity cratons are defined simultaneously using seismic tomographic maps^{2,3,16} in the depth range 200-250 km and geologically defined cratonic outlines⁶ (b), including spatially more extensive area of the two in each particular region. The high viscosity cratons in our models (a) are more extensive than geologically defined cratons (b) and

74 often include several neighboring geologically defined cratonic regions (a), as our models
75 have a wide (~1000 km where possible) regions of interpolations toward the neighboring
76 regions, and merge a number of geologically defined cratonic areas (a). The Australian
77 cratonic region (a) is extended in a way that high-viscosity province also encompasses
78 the Australia-Antarctic discordance zone (AAD), as we were unable to reproduce the
79 correct sign of geoid without AAD having high viscosity in upper mantle. Mantle
80 viscosity wedges are defined as ~1000 km wide zones of lower viscosities that extend
81 from the trench into the backarc region (a), with wider regions defined in the regions of
82 multiple neighboring subduction zones with opposite polarities, such as ones in the SW
83 Pacific (a). We vary viscosity values in depth range 100-250 km in the tectonically
84 regionalized model as it follows: cratons 10^{21} - 10^{22} Pa s, mantle wedges 10^{18} - 10^{19} Pa s,
85 background regions 10^{20} - 10^{21} Pas. Viscosity of the mantle in depth range 250-660 km is
86 kept constant (10^{21} Pas), while the lower mantle viscosity is varied between 10^{22} and 10^{23}
87 Pas. For the models without tectonic regionalization, we adopt 4-layer viscosity structure
88 (d, f) that consists of: lithosphere (viscosity 10^{24} Pas), upper mantle (viscosity varied
89 between 10^{19} and 10^{21} Pas), transition zone (viscosity 10^{21} Pas), and lower mantle
90 (viscosity varied between 10^{22} and 10^{23} Pas). Temperature-dependent viscosity is used for
91 both [types](#) of viscosity parameterization (e-f).

92

Supplementary Figure S3. Geoid predictions for different viscosity models and a constant seismic velocity- density scaling. (a-b) Models with imposed tectonic regionalization; (c-e) Models without tectonic regionalization; (f) Observed geoid; (g) Seismic velocity- density scaling used for models (a-e). First, second and third columns show models with viscosity increase between transition zone and lower mantle of 1:20, 1:60 and 1:100, respectively. Fourth column shows details of radial viscosity structure. All buoyancy anomalies are defined from S20RTS tomography¹. C1 represents correlation coefficient between observed and predicted geoid for whole Earth's surface, and C2 indicates average correlation coefficient in the zones of geoid low.

For models with tectonic regionalization (a-b), low viscosity ratio between transition zone and lower mantle (1:20) always results in geoid prediction that is dominated by degree-2 pattern. High viscosity ratios across 660 km discontinuity of 1:60 to 1:100 yield more realistic predictions for the models with imposed tectonic regionalization (a-b). Lower viscosity of mantle wedges (b) of 10^{18} Pa s results in more positive geoid anomaly in the present-day subduction zones, comparing to higher mantle wedge viscosity of 10^{19} Pa s (a), suggesting that the mantle viscosity wedge could be significantly lower than the surrounding regions. For the models without tectonic regionalization, all models with high viscosity of upper mantle (depth range 100-410 km) yield geoid prediction dominated by degree-2 pattern (c), indicating that upper mantle viscosity has to be lower than 10^{21} Pa s. Models with upper mantle viscosity of 10^{20} Pa s and transition zone viscosity of 10^{21} Pa s (d) yield good predictions of geoid for viscosity ratios across 660 km discontinuity larger than 1:60. Finally, if viscosity of the upper mantle is reduced to

114 10^{19} Pa s (e) predicted geoid patterns are reasonable just for low (1:20 or lower) ratio of
115 transition zone: lower mantle viscosity, but the predicted geoid amplitudes are too high.

116

Supplementary Figure S4. Comparison of geoid prediction for models utilizing S20RTS¹, SB4L18² and TX2005³ tomography models. (a) Geoid predictions centered on Pacific hemisphere; (b) Observed geoid¹⁷ centered on Pacific hemisphere; (c) Seismic velocity-density scaling; (d) Geoid predictions centered on Atlantic hemisphere; (e) Observed geoid centered on Atlantic hemisphere¹⁷, (f) Radial viscosity profile. Ratios 1:40, 1:80 and 1:100 indicate viscosity increase between transition zone and lower mantle. Negative buoyancy in upper mantle is defined based on RUM model¹⁸, while other buoyancy anomalies are defined using seismic velocity- density scaling shown on (c). C1 represents correlation coefficient between observed and predicted geoid for whole Earth's surface, and C2 indicates average correlation coefficient in the zones of geoid low.

For all models, the preferred viscosity ratio across 660 km has to be higher than 1:40, as models with this viscosity ratio have geoid predictions mostly dominated by degree-2 pattern (a, d). For the Pacific and circum-Pacific region, three models yield rather different geoid predictions (a). Models SB4L18² and TX2005³ have more strongly defined central Pacific geoid highs, which relates to stronger tomographic anomaly from the Pacific superplume in the lower mantle (a). Model S20RTS¹ has geoid high translated toward the western Pacific subduction zones, which is more similar to the observations (b). Models SB4L18 and TX2005 are less successful reproducing NE Pacific geoid low, and we therefore prefer model S20RTS for the Pacific region geoid predictions. In addition, predictions of the Ross sea and South Pacific geoid lows are the best obtained by S20RTS model (a). On other hand, S20RTS and SB4L18 models fail reproducing amplitudes of geoid low in the belt extending from Siberia to the Indian Ocean, while

139 TX2005 is more successful in the geoid low prediction in this region. In the region of
140 Atlantic-Africa geoid highs (d), the SB4L18 model seems to be most successful in
141 predicting geoid trends, with two highs centralized in South Africa (presumably related to
142 the African superplume) and Mediterranean-North Atlantic regions (presumably related
143 to Mediterranean subduction and Iceland hotspot). Model S20RTS is less successful
144 reproducing geoid highs in North Atlantic, and South Africa geoid high predicted further
145 north in the central Africa than observed. Model TX2005 on other hand relatively
146 successfully predicts South Africa geoid high, but it fails to adequately reproduce North
147 Atlantic high (d). Since we are mostly interested in the circum-Pacific belt of geoid lows,
148 we utilized S20RTS model for most of the results shown in the main manuscript.

149

149 **Supplementary Figure S5.** Geoid predictions (a-g) for models with different
150 tomography-density scaling functions (i). Observed geoid is shown on (h), colored lines
151 on (i) show scaling functions. Dotted and dashed black lines show range of scaling values
152 suggested by geodynamic (dotted) and mineral physics studies (dashed), based on ¹⁹. All
153 buoyancy anomalies are defined from S20RTS tomography¹. C1 represents correlation
154 coefficient between observed and predicted geoid for whole Earth's surface, and C2
155 indicates average correlation coefficient in the zones of geoid low.

156 Although we significantly vary depth-dependent seismic velocity- density scaling,
157 difference in the geoid prediction is smaller than when viscosity model (Supplementary
158 Fig. S3) or seismic model (Supplementary Fig. S4) are varied. For example, the model
159 with constant scaling of 0.2 (b) yields similarly well-predicted geoid as some of more
160 complex scaling functions (e.g. d, f).

161

Supplementary Figure S6. Impact of lateral and vertical resolution on geoid prediction for two models without tectonic regionalization (a-b) having different radial viscosity structure (c) and same seismic velocity- density scaling (d). First and second column show geoid predictions centered on Pacific and African hemisphere, respectively. Third column shows predicted dynamic topography. CitcomS global models use 12 caps for the whole globe, and the resolution is defined for each cap. We test two different lateral resolutions: 129x129 (approximately 50 km) and 257x257 (approximately 25 km). In the radial directions we test two resolutions: 65 nodes (approximately 44 km) and 129 nodes in the whole mantle (approximately 22 km), with nodes uniformly distributed in the radial direction. All buoyancy anomalies are defined from S20RTS tomography¹.

We find a slight difference (a-b) in geoid predictions between models that have different vertical resolution (129x129x65 vs. 129x129x129), while there seems to be no difference in geoid prediction between models that have 22 km vertical resolution and different lateral resolution (129x129x129 vs. 257x257x129). However, all patterns and trends of geoid predictions are essentially the same for all resolutions we tested. We attribute the difference in the geoid prediction between models having 44 km and 22 km resolution to the slightly different density/temperature models used [as input data](#). Namely, the higher radial resolution models essentially sample tomography at two times denser interval, therefore introducing slightly different additional content in the density field, which is reflected in the geoid prediction.

181 **Supplementary Table 1.** Comparison of observed and model geoid minima

	Northeast Pacific			West Atlantic			Indian Ocean			Ross Sea		
	Lon.	Lat.	Amp.	Lon.	Lat.	Amp.	Lon.	Lat.	Amp.	Lon.	Lat.	Amp.
	° E	° N	m	° E	° N	m	° E	° N	m	° E	° N	m
Observed*	239	22	-46	295	23	-52	78 107	3 -32	-102 -38	188	-72	-63
Model A	224	41	-69	310	23	-47	96	-22	-75	186 252	-58 -49	-75 -52
Model B	224	45	-45	307	22	-45	95	-19	-65	180 225 261	-58 -69 -50	-48 -42 -43
Model C	265	11	-26	306 311	22 -11	-29 -32	88	-7	-63	170 264	-59 -58	-28 -39

182 *Filtered to remove features <1000 km in size.

183 Note: The Hudson Bay anomaly is not compared due to its partial glacial rebound origin.

184

185 Supplementary Table 1 shows amplitudes of observed and model geoid minima for the
186 preferred model (Fig. 2), obtained for viscosity structure shown on Fig. 3b (viscosity ratio
187 at 660 km is 1:100) and seismic velocity-to-density scaling shown on Fig. 3g. Model A
188 corresponds to the best-fitting model shown on Fig. 2a, while models B and C correspond
189 to the models shown on Figs. 2b-c, having upwellings removed from the best-fitting
190 model from depths 0-660 km (B) and 0-1000 km (C). Amplitudes of geoid minima are
191 evaluated at the several locations for observed and predicted models, with the coordinates
192 shown in the table and general location of the zones of localized geoid lows shown on
193 Fig. 2a-d. There is a good agreement between observed and predicted geoid amplitudes

194 for the best fitting model (Model A; Fig. 2a). Once the upwellings are removed from the
195 upper mantle (Model B, Fig. 2b) and 0-1000 km depth (Model C, Fig. 2c), the amplitude
196 fit becomes worse.

197

197 **Supplementary Table S2.** Model parameters held constant in our runs.

Parameter	Symbol	Value
Ambient mantle density	ρ_m	3340 kg/m ³
Reference viscosity	η_o	1x10 ²¹ Pa s
Thermal diffusivity	κ	10 ⁻⁶ m ² /s
Coefficient of thermal expansion	α	3x10 ⁻⁵ 1/K
Gravitational acceleration	g	9.81 m/s ²
Earth's radius	R	6371 km
Rayleigh number	Ra	7.5x10 ⁷

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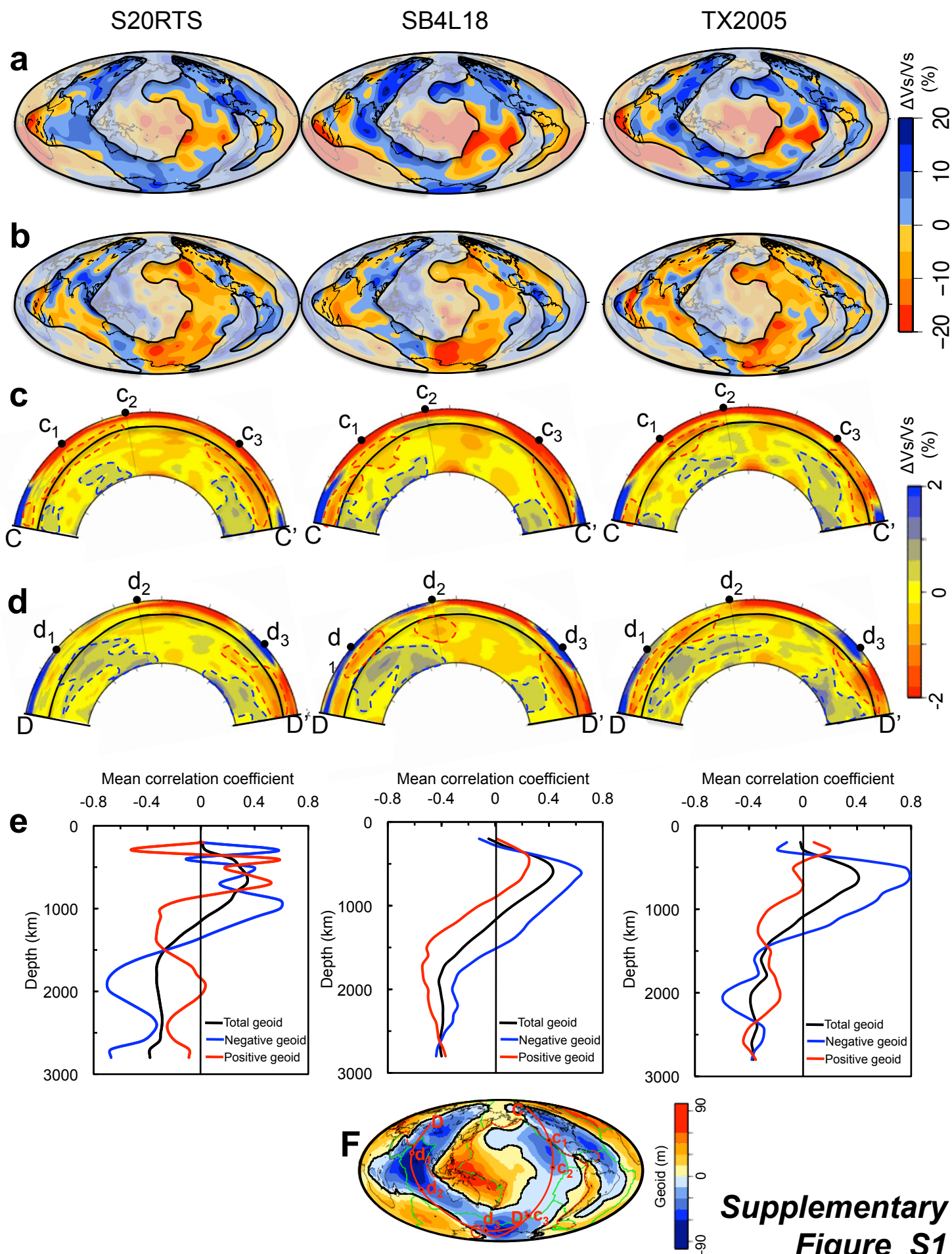
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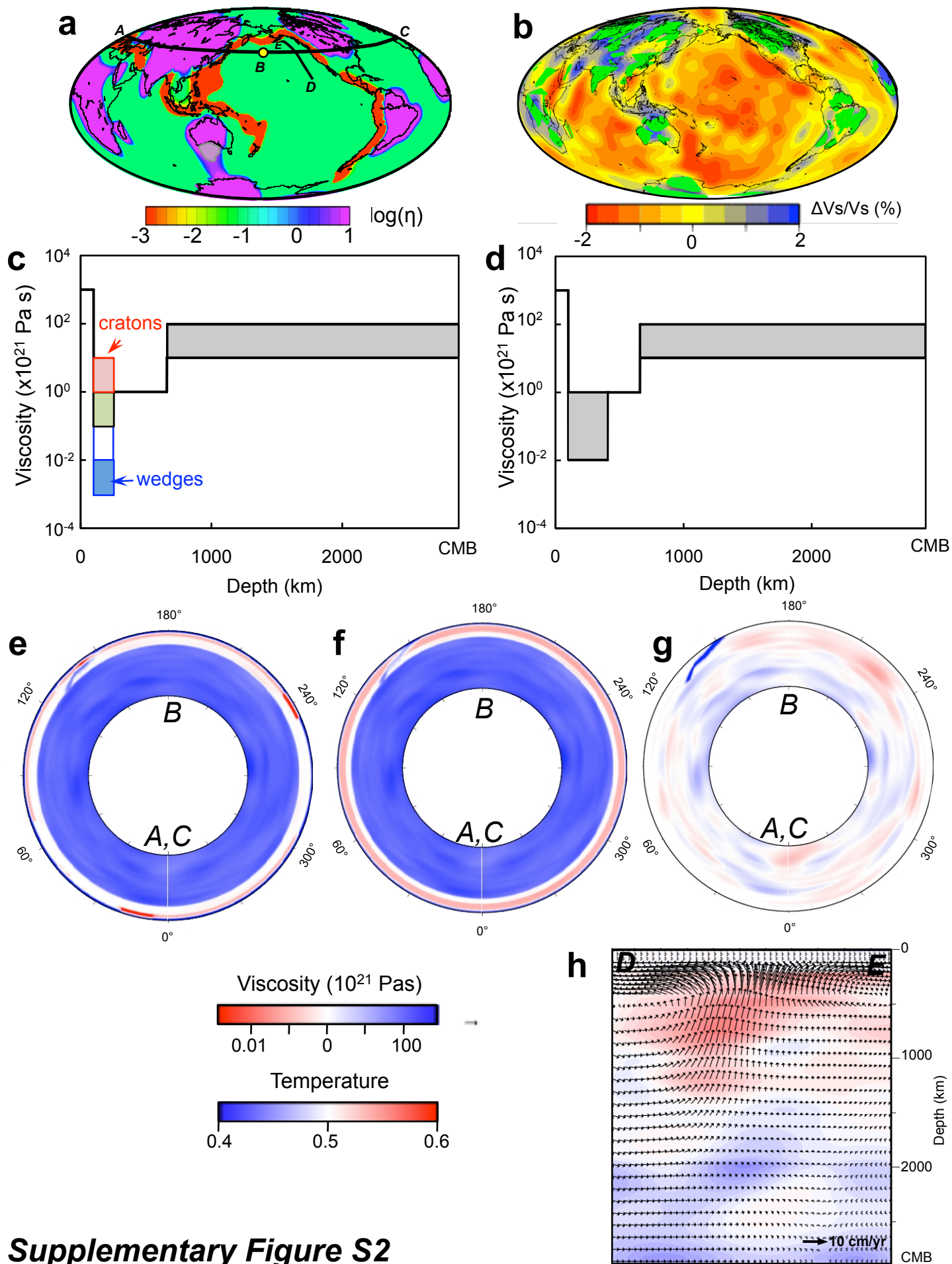
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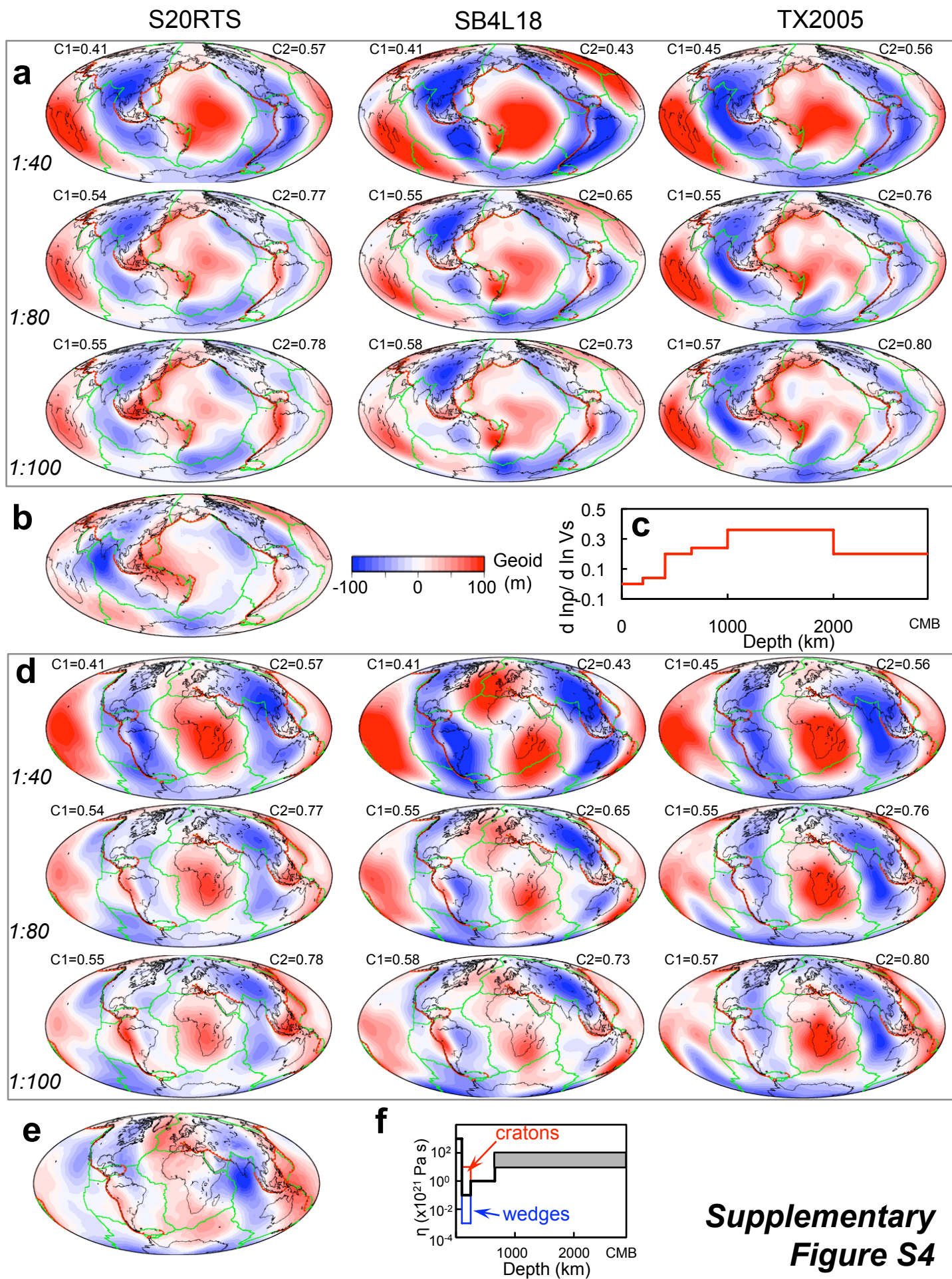
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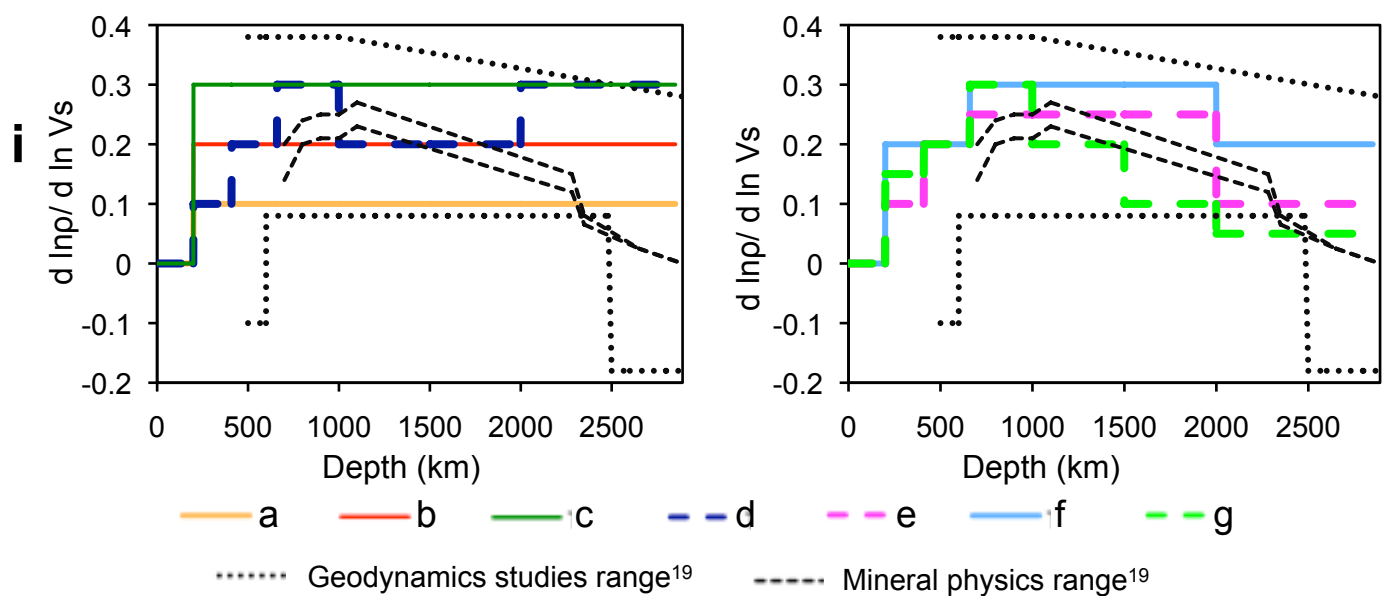
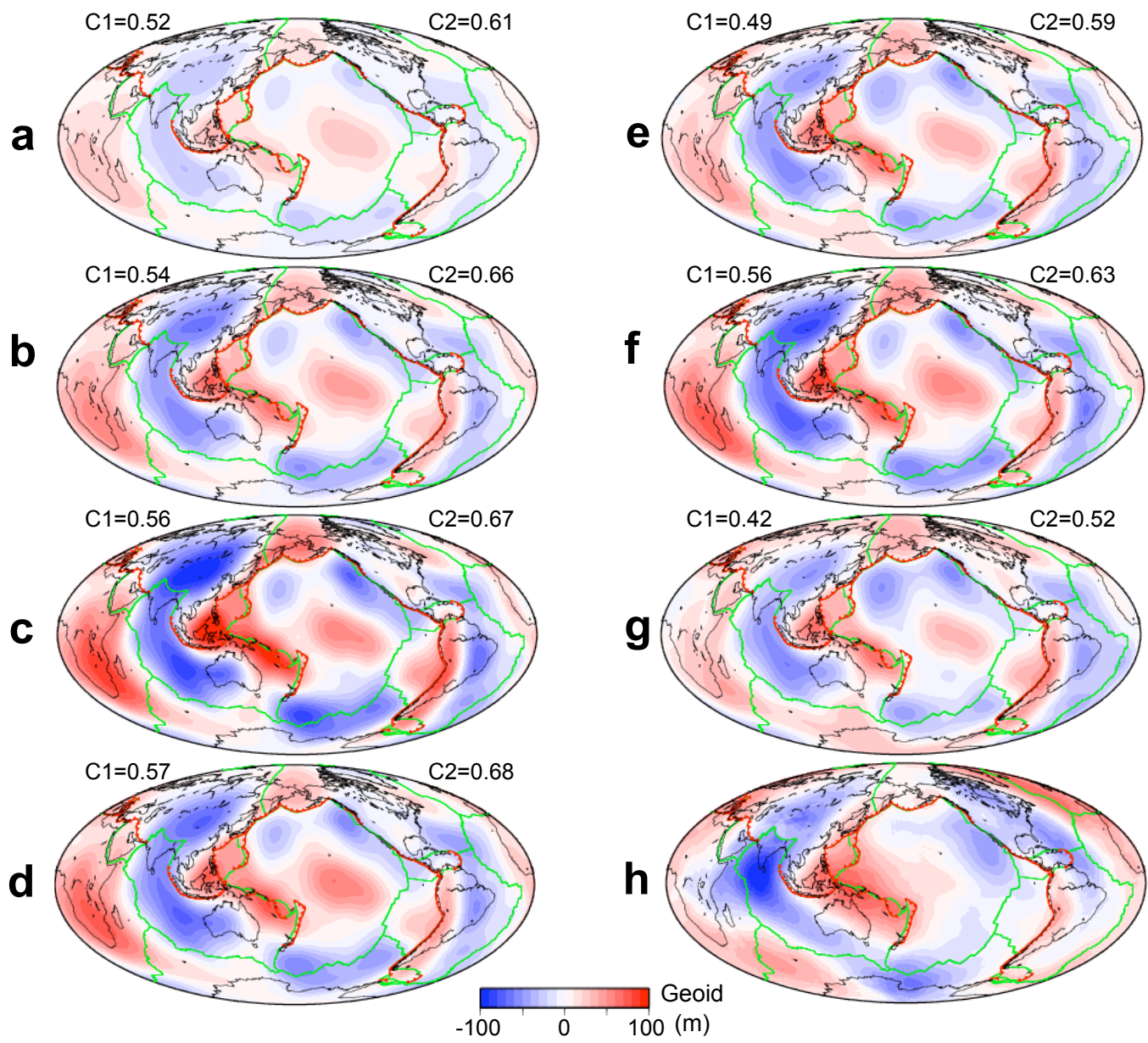


**Supplementary
Figure S1**

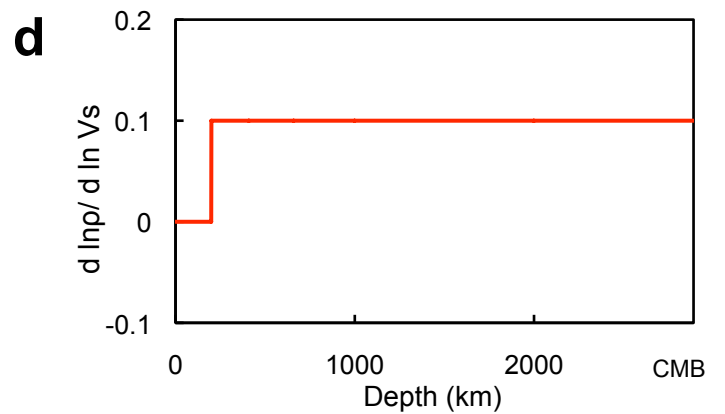
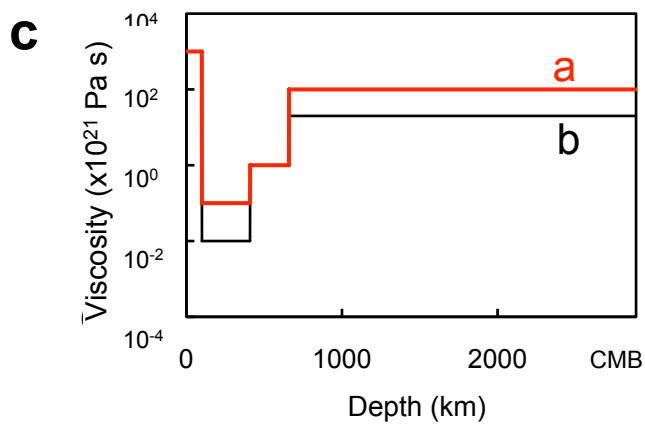
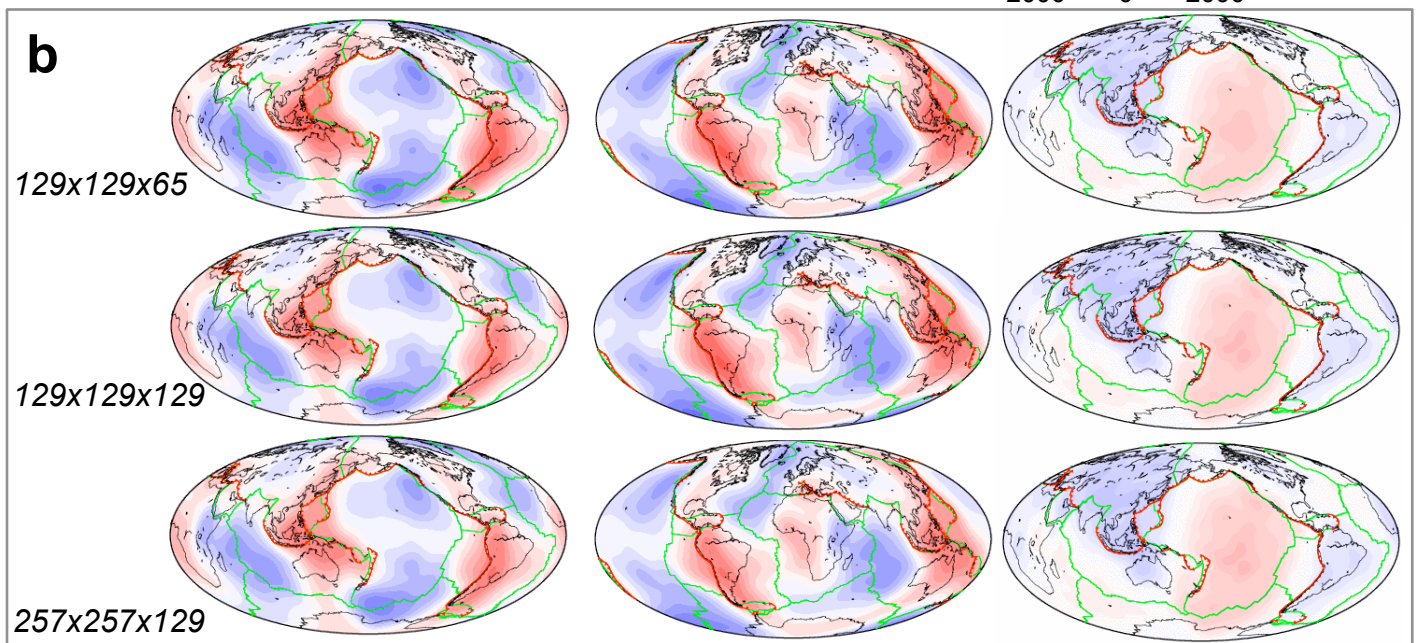
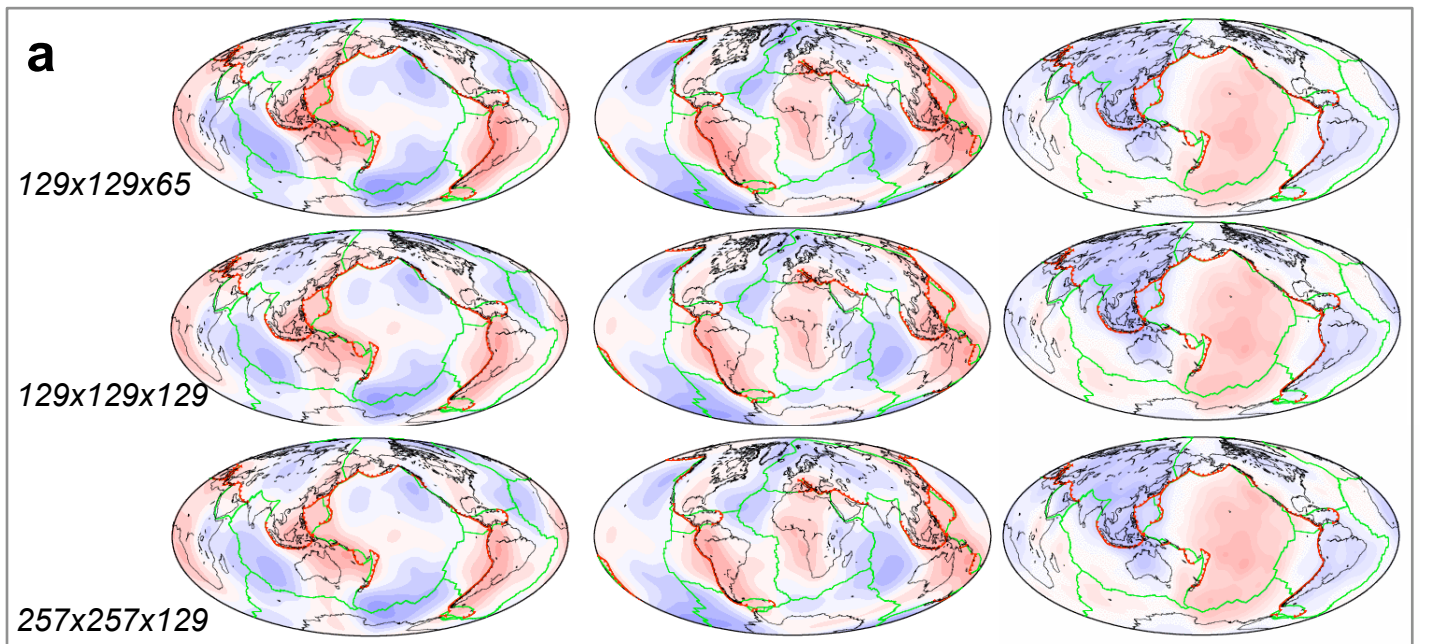


Supplementary Figure S2





Supplementary Figure S5



Supplementary Figure S6