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## **Mantle upwellings**

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### **above slab graveyards linked to the global geoid lows**

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## **SUPPLEMENTARY MATERIAL**

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14        **Supplementary Figure S1.** Details of velocity structure for models S20RTS<sup>1</sup> (first  
15 column) and SB4L18<sup>2</sup> (second column), and model TX2005<sup>3</sup> (third column) in the zones  
16 of geoid minima. (a) Integrated tomography in depth range 2050-2850 km; (b) Integrated  
17 tomography in depth range 300-1000 km; (c) Cross section from North America to Ross  
18 Sea; (d) Cross section from central Asia to Ross Sea; (e) Correlation coefficient between  
19 observed geoid and tomography calculated at every 100 km depth; (f) Observed geoid.  
20 Semi-transparent outlines on (a-b) cover zone of global geoid high; blue and red dashed  
21 lines (c-d) indicate lower mantle high velocity and upper-to-mid mantle low velocity  
22 anomalies of interest, respectively; black, blue and red lines on (e) show mean correlation  
23 coefficient between whole geoid, areas of negative geoid and areas of positive geoid,  
24 respectively; red lines on (f) indicate position of great circle cross-sections intersecting  
25 geoid low. Correlation coefficient between observed geoid and tomography models (e) is  
26 calculated as a product of values divided by product of standard deviations at every 100  
27 km depth. The mean value of correlation coefficient is than calculated for whole geoid,  
28 areas of geoid lows, and geoid highs.

29

30 Integrated tomography plots (a-b) show a correlation between geoid low (f) and both  
31 seismically fast regions in lower mantle (a) and slow regions in upper-to-mid mantle (b)  
32 for all investigated tomography models. In the region of NE Pacific geoid low, all models  
33 define a seismically fast anomaly in the lower 500-1000 km of mantle (c), which is  
34 probably related to an ancient subducted slab that hasn't been recognized previously,  
35 except by analysis of SKS-SKKS splitting discrepancies<sup>4</sup>. A zone of upper-mid mantle  
36 seismically slow velocities is located above this fast anomaly (c), model SB4L18<sup>2</sup> defines

37 this structure largely in the lower mantle, while models S20RTS<sup>1</sup> and TX2005<sup>3</sup> place it at  
38 depths up to 800 km. In the Ross Sea region (c-d), all models show coherent upper-mid  
39 mantle seismically slow region. Fast seismic anomaly in the lower mantle appears to  
40 consist of several separate structures, possibly corresponding to different stages of  
41 Gondwana subduction. In the zone of Indian Ocean geoid low, all models clearly define  
42 fast seismic anomalies in the lower mantle (d), that was previously attributed to Mesozoic  
43 Tethyan subduction<sup>5</sup>. In the upper-to-mid mantle, TX2005 defines the most coherent  
44 slow region in depth range of 300-800 km (d) in the region of local geoid low (10°S to  
45 10°N), while models S20RTS and SB4L18 show no particularly distinctive region of  
46 slow velocities (d). Correlation analysis between observed geoid tomography and various  
47 component of geoid (e) indicate that negative geoid is correlated with low velocity  
48 tomographic anomalies in upper 1200-1500 km of mantle and high velocity seismic  
49 anomalies in the lower mantle. Positive geoid is correlated with high velocity anomalies  
50 in upper 800 km of mantle and negative seismic anomalies in the lower mantle.

51

51 **Supplementary Figure S2.** Details of viscosity structure. (a) Tectonic regionalization  
52 map with high viscosity cratons, low viscosity mantle wedges and intermediate viscosity  
53 background regions; (b) S20RTS tomography at 250 km depth with outlines (green) of  
54 geologically defined cratons<sup>6</sup>; (c) Radial viscosity structure for models with tectonic  
55 regionalization; (d) Radial viscosity structure for models without tectonic regionalization;  
56 (e-f) Viscosity cross-sections for models with (e) and without (f) tectonic regionalization;  
57 (g) Global temperature cross-section; (h) Regional cross-section through NE Pacific  
58 geoid low with velocity vectors overlay. Position of cross-sections (e-h) is shown with  
59 black line on (a); red, green and blue rectangles on (c) show upper mantle range of  
60 viscosities for cratons, background and wedges, respectively; grey rectangles on (c-d)  
61 show range of viscosities in lower and upper mantle.

62 Following the experience from previous studies that use scaled tomographic models for  
63 geoid and gravity predictions to either define only the best fitting radial viscosity  
64 structure<sup>7,8,9,10,11</sup>, without imposing any lateral tectonic viscosity parameterization, or  
65 models in which viscosity is not just a function of depth and temperature (seismic  
66 velocity), but also have pre-imposed large-scale variations based on upper mantle  
67 structure and tectonics<sup>12,13,14,15</sup>, we develop two types of models: (1) models with tectonic  
68 regionalization in the upper mantle (a-c, e), and (2) models without tectonic  
69 regionalization in the upper mantle (d, f). For models with tectonic regionalization, high  
70 viscosity cratons are defined simultaneously using seismic tomographic maps<sup>2,3,16</sup> in the  
71 depth range 200-250 km and geologically defined cratonic outlines<sup>6</sup> (b), including  
72 spatially more extensive area of the two in each particular region. The high viscosity  
73 cratons in our models (a) are more extensive than geologically defined cratons (b) and

74 often include several neighboring geologically defined cratonic regions (a), as our models  
75 have a wide (~1000 km where possible) regions of interpolations toward the neighboring  
76 regions, and merge a number of geologically defined cratonic areas (a). The Australian  
77 cratonic region (a) is extended in a way that high-viscosity province also encompasses  
78 the Australia-Antarctic discordance zone (AAD), as we were unable to reproduce the  
79 correct sign of geoid without AAD having high viscosity in upper mantle. Mantle  
80 viscosity wedges are defined as ~1000 km wide zones of lower viscosities that extend  
81 from the trench into the backarc region (a), with wider regions defined in the regions of  
82 multiple neighboring subduction zones with opposite polarities, such as ones in the SW  
83 Pacific (a). We vary viscosity values in depth range 100-250 km in the tectonically  
84 regionalized model as it follows: cratons  $10^{21}$ -  $10^{22}$  Pa s, mantle wedges  $10^{18}$ - $10^{19}$  Pa s,  
85 background regions  $10^{20}$ -  $10^{21}$  Pas. Viscosity of the mantle in depth range 250-660 km is  
86 kept constant ( $10^{21}$  Pas), while the lower mantle viscosity is varied between  $10^{22}$  and  $10^{23}$   
87 Pas. For the models without tectonic regionalization, we adopt 4-layer viscosity structure  
88 (d, f) that consists of: lithosphere (viscosity  $10^{24}$  Pas), upper mantle (viscosity varied  
89 between  $10^{19}$  and  $10^{21}$  Pas), transition zone (viscosity  $10^{21}$  Pas), and lower mantle  
90 (viscosity varied between  $10^{22}$  and  $10^{23}$  Pas). Temperature-dependent viscosity is used for  
91 both [types](#) of viscosity parameterization (e-f).

92

92 **Supplementary Figure S3.** Geoid predictions for different viscosity models and a  
93 constant seismic velocity- density scaling. (a-b) Models with imposed tectonic  
94 regionalization; (c-e) Models without tectonic regionalization; (f) Observed geoid; (g)  
95 Seismic velocity- density scaling used for models (a-e). First, second and third columns  
96 show models with viscosity increase between transition zone and lower mantle of 1:20,  
97 1:60 and 1:100, respectively. Fourth column shows details of radial **viscosity** structure.  
98 All buoyancy anomalies are defined from S20RTS tomography<sup>1</sup>. C1 represents  
99 correlation coefficient between observed and predicted geoid for whole Earth's surface,  
100 and C2 indicates average correlation coefficient in the zones of geoid low.

101 For models with tectonic regionalization (a-b), low viscosity ratio between transition  
102 zone and lower mantle (1:20) always results in geoid prediction that is dominated by  
103 degree-2 pattern. High viscosity ratios across 660 km discontinuity of 1:60 to 1:100 yield  
104 more realistic predictions for the models with imposed tectonic regionalization (a-b).  
105 Lower viscosity of mantle wedges (b) of  $10^{18}$  Pa s results in more positive geoid anomaly  
106 in the present-day subduction zones, comparing to higher mantle wedge viscosity of  $10^{19}$   
107 Pa s (a), suggesting that the mantle viscosity wedge could be significantly lower than the  
108 surrounding regions. For the models without tectonic regionalization, all models with  
109 high viscosity of upper mantle (depth range 100-410 km) yield geoid prediction  
110 dominated by degree-2 pattern (c), indicating that upper mantle viscosity has to be lower  
111 than  $10^{21}$  Pa s. Models with upper mantle viscosity of  $10^{20}$  Pa s and transition zone  
112 viscosity of  $10^{21}$  Pa s (d) yield good predictions of geoid for viscosity ratios across 660  
113 km discontinuity larger than 1:60. Finally, if viscosity of the upper mantle is reduced to

114  $10^{19}$  Pa s (e) predicted geoid patterns are reasonable just for low (1:20 or lower) ratio of  
115 transition zone: lower mantle viscosity, but the predicted geoid amplitudes are too high.

116

116 **Supplementary Figure S4.** Comparison of geoid prediction for models utilizing  
117 S20RTS<sup>1</sup>, SB4L18<sup>2</sup> and TX2005<sup>3</sup> tomography models. (a) Geoid predictions centered on  
118 Pacific hemisphere; (b) Observed geoid<sup>17</sup> centered on Pacific hemisphere; (c) Seismic  
119 velocity-density scaling; (d) Geoid predictions centered on Atlantic hemisphere; (e)  
120 Observed geoid centered on Atlantic hemisphere<sup>17</sup>, (f) Radial viscosity profile. Ratios  
121 1:40, 1:80 and 1:100 indicate **viscosity** increase between transition zone and lower  
122 mantle. Negative buoyancy in upper mantle is defined based on RUM model<sup>18</sup>, while  
123 other buoyancy anomalies are defined using seismic velocity- density scaling shown on  
124 (c). C1 represents correlation coefficient between observed and predicted geoid for whole  
125 Earth's surface, and C2 indicates average correlation coefficient in the zones of geoid  
126 low.

127 For all models, the preferred viscosity ratio across 660 km has to be higher than 1:40, as  
128 models with this viscosity ratio have geoid predictions mostly dominated by degree-2  
129 pattern (a, d). For the Pacific and circum-Pacific region, three models yield rather  
130 different geoid predictions (a). Models SB4L18<sup>2</sup> and TX2005<sup>3</sup> have more strongly  
131 defined central Pacific geoid highs, which relates to stronger tomographic anomaly from  
132 the Pacific superplume in the lower mantle (a). Model S20RTS<sup>1</sup> has geoid high translated  
133 toward the western Pacific subduction zones, which is more similar to the observations  
134 (b). Models SB4L18 and TX2005 are less successful reproducing NE Pacific geoid low,  
135 and we therefore prefer model S20RTS for the Pacific region geoid predictions. In  
136 addition, predictions of the Ross sea and South Pacific geoid lows are the best obtained  
137 by S20RTS model (a). On other hand, S20RTS and SB4L18 models fail reproducing  
138 amplitudes of geoid low in the belt extending from Siberia to the Indian Ocean, while

139 TX2005 is more successful in the geoid low prediction in this region. In the region of  
140 Atlantic-Africa geoid highs (d), the SB4L18 model seems to be most successful in  
141 predicting geoid trends, with two highs centralized in South Africa (presumably related to  
142 the African superplume) and Mediterranean-North Atlantic regions (presumably related  
143 to Mediterranean subduction and Iceland hotspot). Model S20RTS is less successful  
144 reproducing geoid highs in North Atlantic, and South Africa geoid high predicted further  
145 north in the central Africa than observed. Model TX2005 on other hand relatively  
146 successfully predicts South Africa geoid high, but it fails to adequately reproduce North  
147 Atlantic high (d). Since we are mostly interested in the circum-Pacific belt of geoid lows,  
148 we utilized S20RTS model for most of the results shown in the main manuscript.

149

149 **Supplementary Figure S5.** Geoid predictions (a-g) for models with different  
150 tomography-density scaling functions (i). Observed geoid is shown on (h), colored lines  
151 on (i) show scaling functions. Dotted and dashed black lines show range of scaling values  
152 suggested by geodynamic (dotted) and mineral physics studies (dashed), based on <sup>19</sup>. All  
153 buoyancy anomalies are defined from S20RTS tomography<sup>1</sup>. C1 represents correlation  
154 coefficient between observed and predicted geoid for whole Earth's surface, and C2  
155 indicates average correlation coefficient in the zones of geoid low.

156 Although we significantly vary depth-dependent seismic velocity- density scaling,  
157 difference in the geoid prediction is smaller than when viscosity model (Supplementary  
158 Fig. S3) or seismic model (Supplementary Fig. S4) are varied. For example, the model  
159 with constant scaling of 0.2 (b) yields similarly well-predicted geoid as some of more  
160 complex scaling functions (e.g. d, f).

161

161 **Supplementary Figure S6.** Impact of lateral and vertical resolution on geoid prediction  
162 for two models without tectonic regionalization (a-b) having different radial viscosity  
163 structure (c) and same seismic velocity- density scaling (d). First and second column  
164 show geoid predictions centered on Pacific and African hemisphere, respectively. Third  
165 column shows predicted dynamic topography. CitcomS global models use 12 caps for the  
166 whole globe, and the resolution is defined for each cap. We test two different lateral  
167 resolutions: 129x129 (approximately 50 km) and 257x257 (approximately 25 km). In the  
168 radial directions we test two resolutions: 65 nodes (approximately 44 km) and 129 nodes  
169 in the whole mantle (approximately 22 km), with nodes uniformly distributed in the  
170 radial direction. All buoyancy anomalies are defined from S20RTS tomography<sup>1</sup>.

171 We find a slight difference (a-b) in geoid predictions between models that have different  
172 vertical resolution (129x129x65 vs. 129x129x129), while there seems to be no difference  
173 in geoid prediction between models that have 22 km vertical resolution and different  
174 lateral resolution (129x129x129 vs. 257x257x129). However, all patterns and trends of  
175 geoid predictions are essentially the same for all resolutions we tested. We attribute the  
176 difference in the geoid prediction between models having 44 km and 22 km resolution to  
177 the slightly different density/temperature models used [as input data](#). Namely, the higher  
178 radial resolution models essentially sample tomography at two times denser interval,  
179 therefore introducing slightly different additional content in the density field, which is  
180 reflected in the geoid prediction.

181

181 **Supplementary Table 1.** Comparison of observed and model geoid minima

|           | <b>Northeast Pacific</b> |      |      | <b>West Atlantic</b> |      |      | <b>Indian Ocean</b> |      |      | <b>Ross Sea</b> |      |      |
|-----------|--------------------------|------|------|----------------------|------|------|---------------------|------|------|-----------------|------|------|
|           | Lon.                     | Lat. | Amp. | Lon.                 | Lat. | Amp. | Lon.                | Lat. | Amp. | Lon.            | Lat. | Amp. |
|           | ° E                      | ° N  | m    | ° E                  | ° N  | m    | ° E                 | ° N  | m    | ° E             | ° N  | m    |
| Observed* | 239                      | 22   | -46  | 295                  | 23   | -52  | 78                  | 3    | -102 | 188             | -72  | -63  |
|           |                          |      |      |                      |      |      | 107                 | -32  | -38  |                 |      |      |
| Model A   | 224                      | 41   | -69  | 310                  | 23   | -47  | 96                  | -22  | -75  | 186             | -58  | -75  |
|           |                          |      |      |                      |      |      |                     |      |      | 252             | -49  | -52  |
| Model B   | 224                      | 45   | -45  | 307                  | 22   | -45  | 95                  | -19  | -65  | 180             | -58  | -48  |
|           |                          |      |      |                      |      |      |                     |      |      | 225             | -69  | -42  |
|           |                          |      |      |                      |      |      |                     |      |      | 261             | -50  | -43  |
| Model C   | 265                      | 11   | -26  | 306                  | 22   | -29  | 88                  | -7   | -63  | 170             | -59  | -28  |
|           |                          |      |      | 311                  | -11  | -32  |                     |      |      | 264             | -58  | -39  |

182 \*Filtered to remove features <1000 km in size.

183 Note: The Hudson Bay anomaly is not compared due to its partial glacial rebound origin.

184

185 Supplementary Table 1 shows amplitudes of observed and model geoid minima for the  
 186 preferred model (Fig. 2), obtained for viscosity structure shown on Fig. 3b (viscosity ratio  
 187 at 660 km is 1:100) and seismic velocity-to-density scaling shown on Fig. 3g. Model A  
 188 corresponds to the best-fitting model shown on Fig. 2a, while models B and C correspond  
 189 to the models shown on Figs. 2b-c, having upwellings removed from the best-fitting  
 190 model from depths 0-660 km (B) and 0-1000 km (C). Amplitudes of geoid minima are  
 191 evaluated at the several locations for observed and predicted models, with the coordinates  
 192 shown in the table and general location of the zones of localized geoid lows shown on  
 193 Fig. 2a-d. There is a good agreement between observed and predicted geoid amplitudes

194 for the best fitting model (Model A; Fig. 2a). Once the upwellings are removed from the  
195 upper mantle (Model B, Fig. 2b) and 0-1000 km depth (Model C, Fig. 2c), the amplitude  
196 fit becomes worse.

197

197 **Supplementary Table S2.** Model parameters held constant in our runs.

| Parameter                        | Symbol   | Value                              |
|----------------------------------|----------|------------------------------------|
| Ambient mantle density           | $\rho_m$ | 3340 kg/m <sup>3</sup>             |
| Reference viscosity              | $\eta_o$ | 1x10 <sup>21</sup> Pa s            |
| Thermal diffusivity              | $\kappa$ | 10 <sup>-6</sup> m <sup>2</sup> /s |
| Coefficient of thermal expansion | $\alpha$ | 3x10 <sup>-5</sup> 1/K             |
| Gravitational acceleration       | $g$      | 9.81 m/s <sup>2</sup>              |
| Earth's radius                   | $R$      | 6371 km                            |
| Rayleigh number                  | $Ra$     | 7.5x10 <sup>7</sup>                |

198

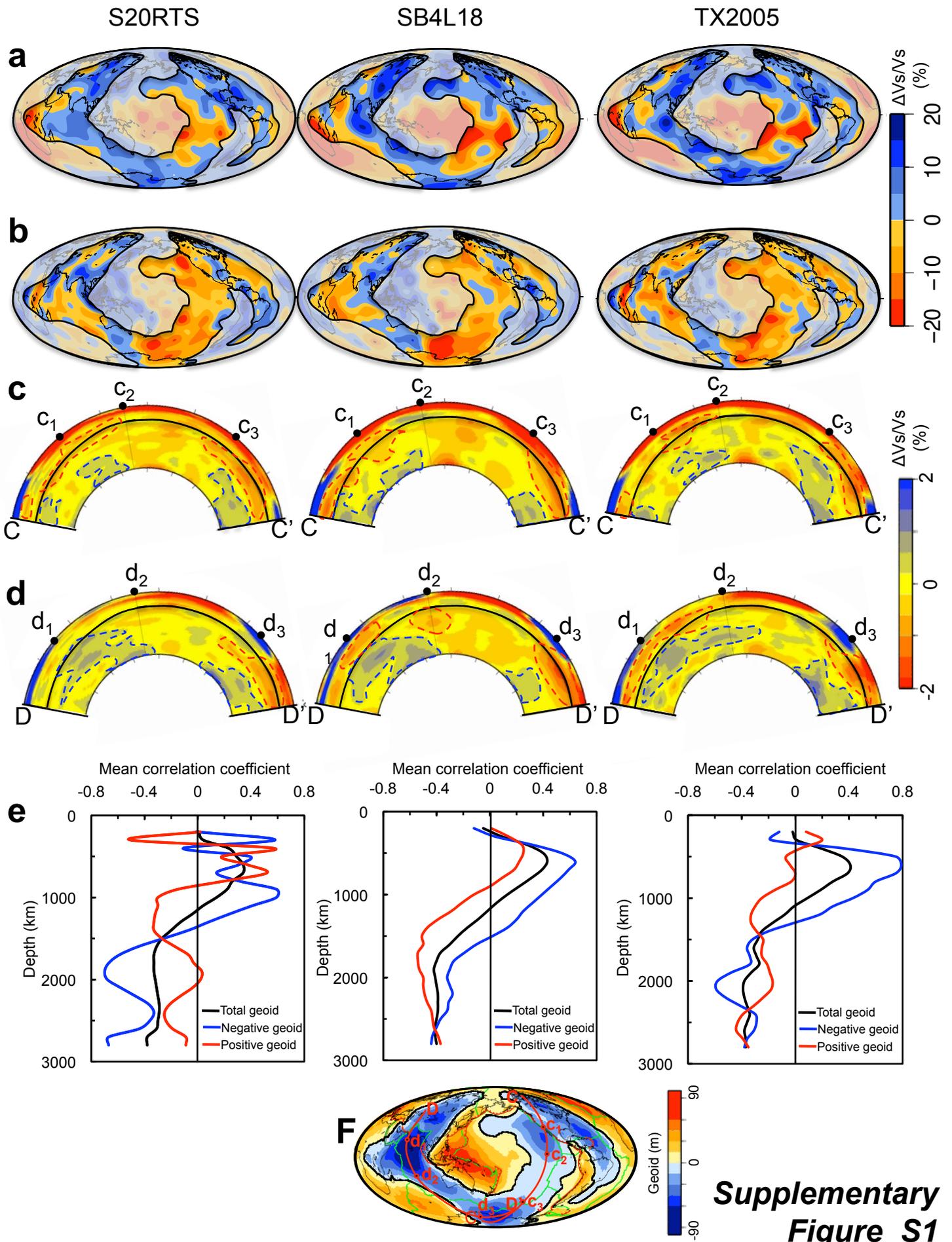
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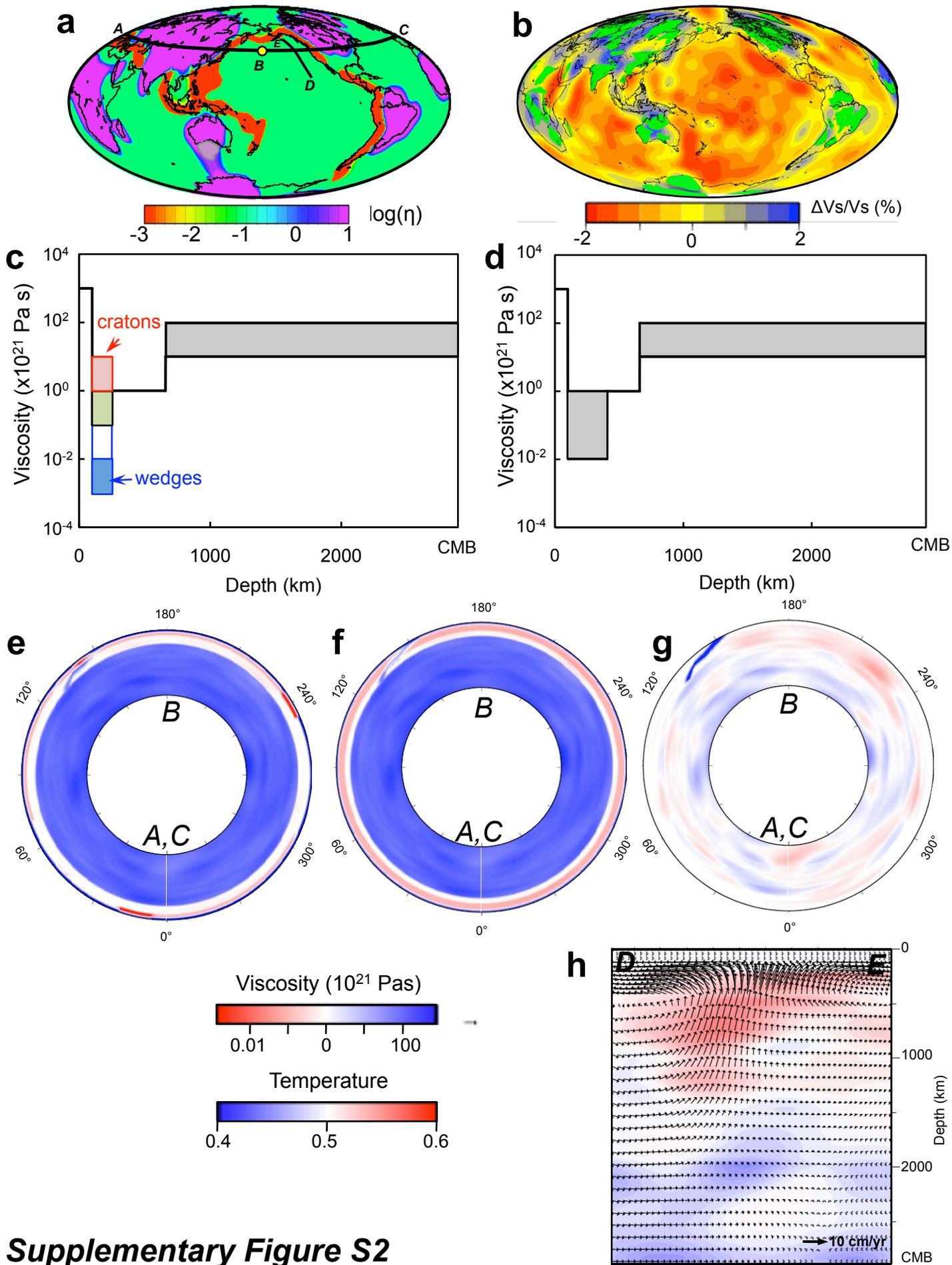
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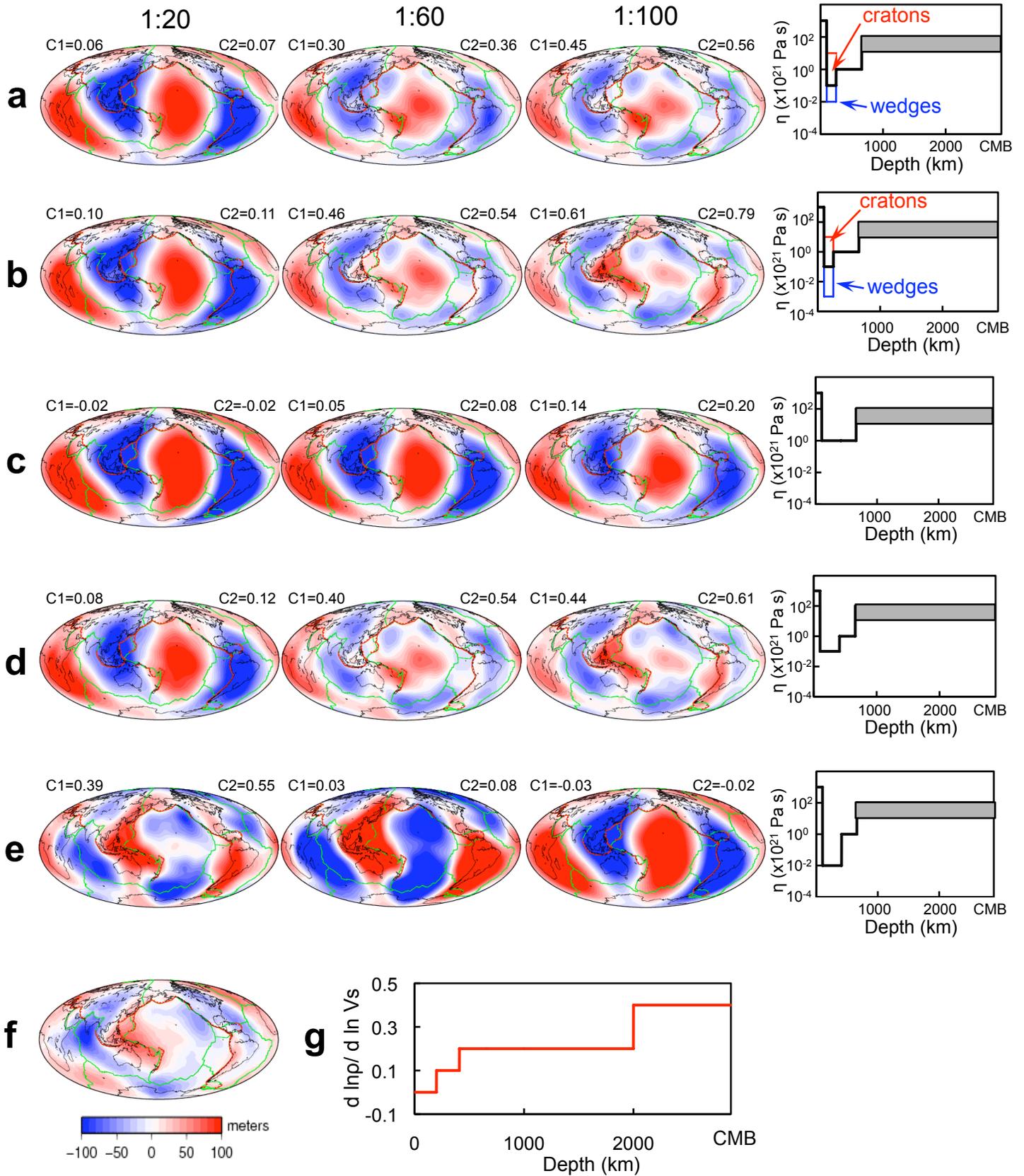
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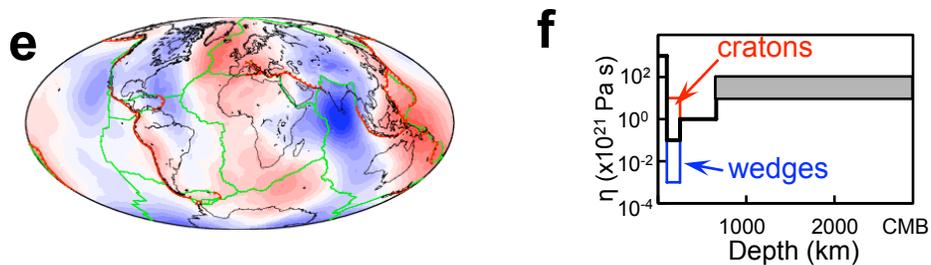
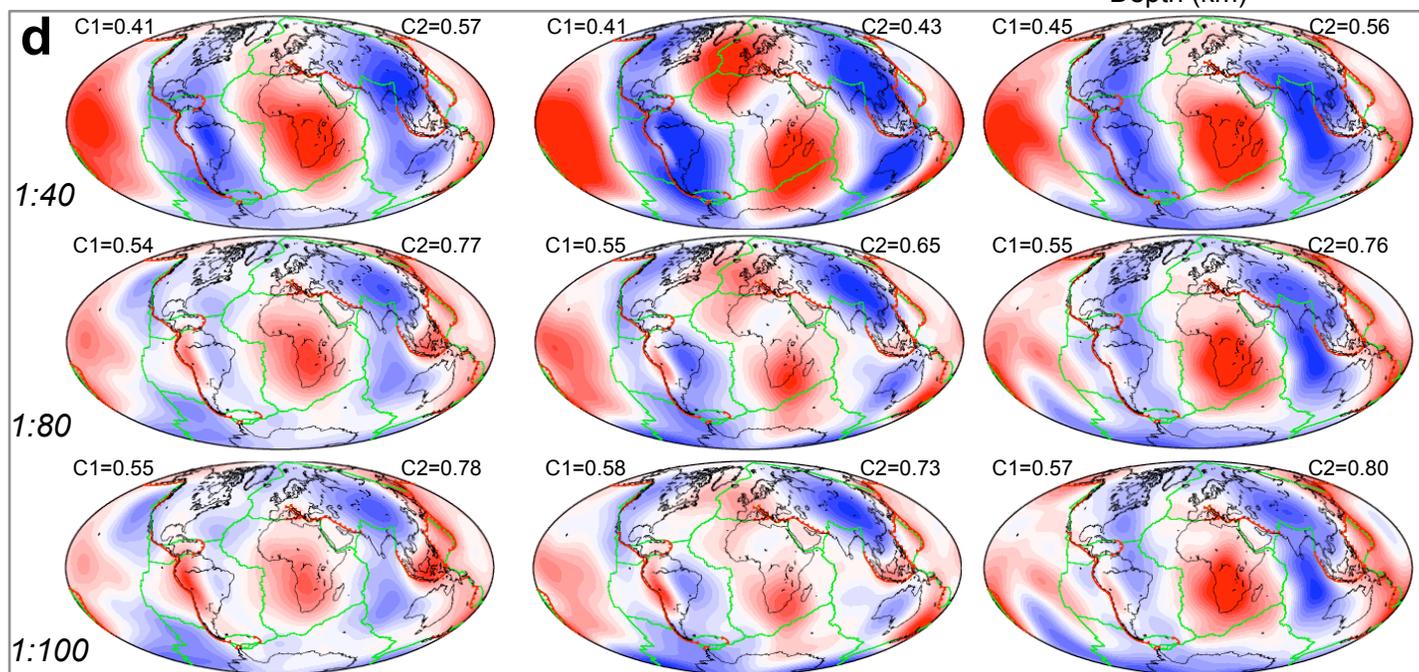
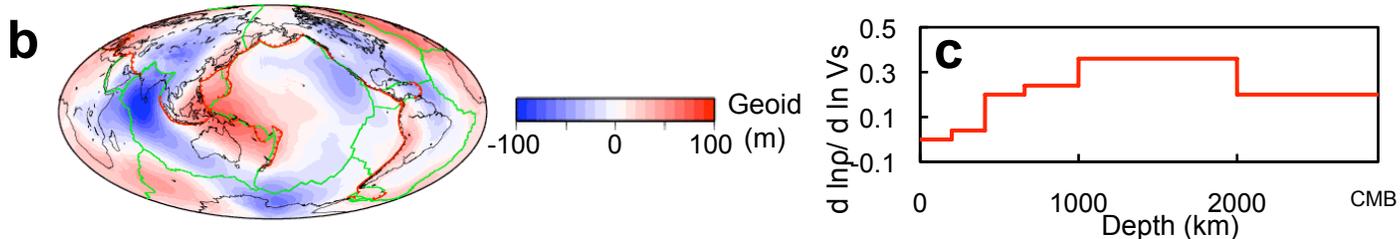
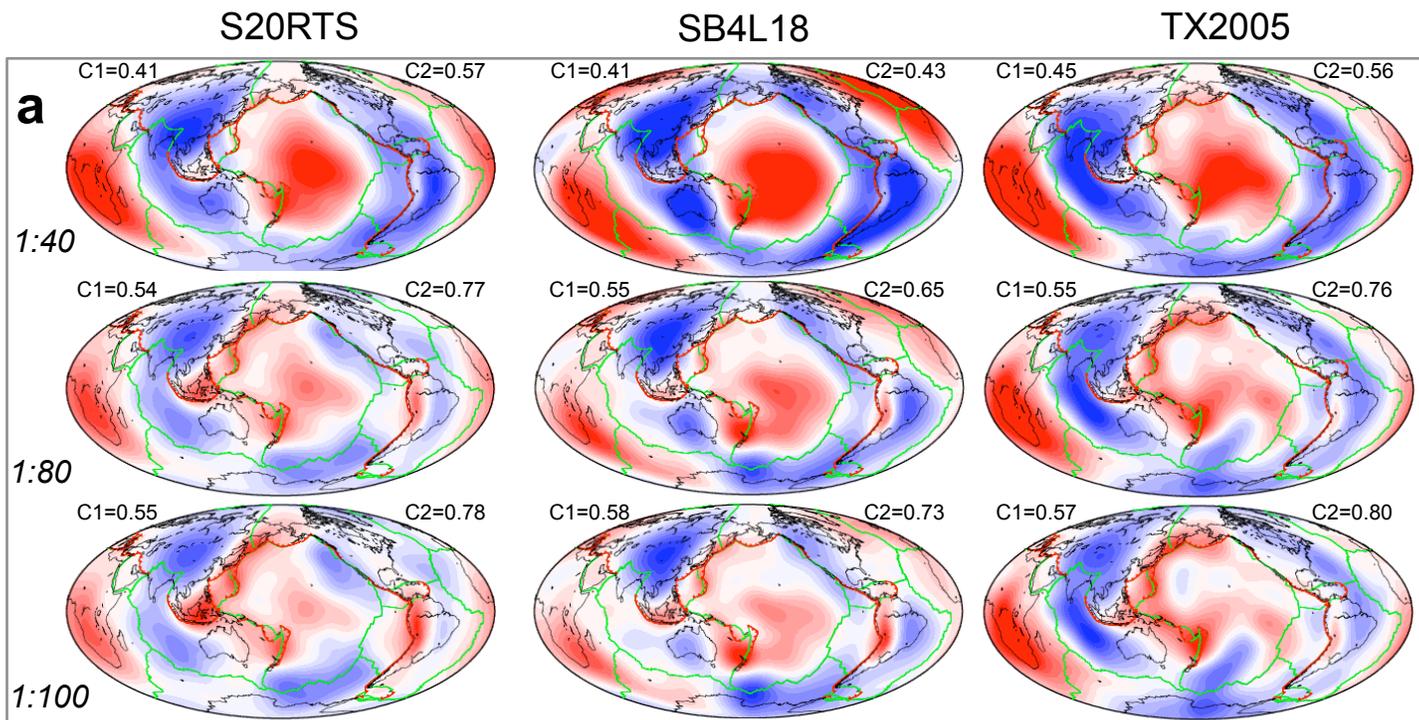




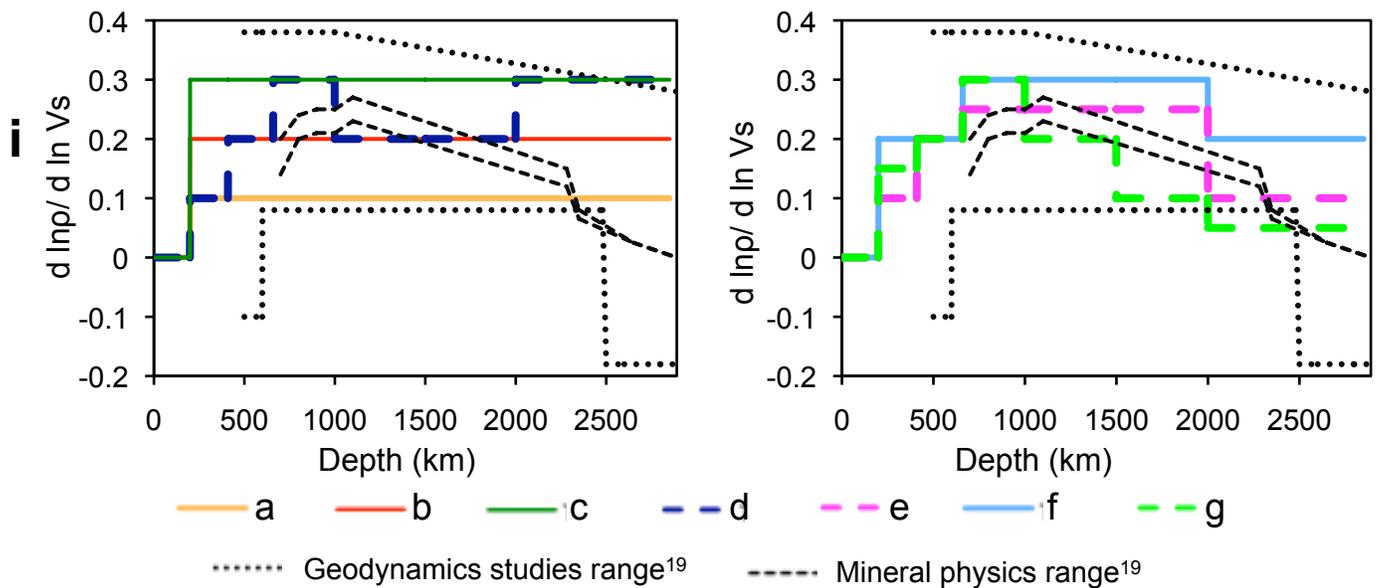
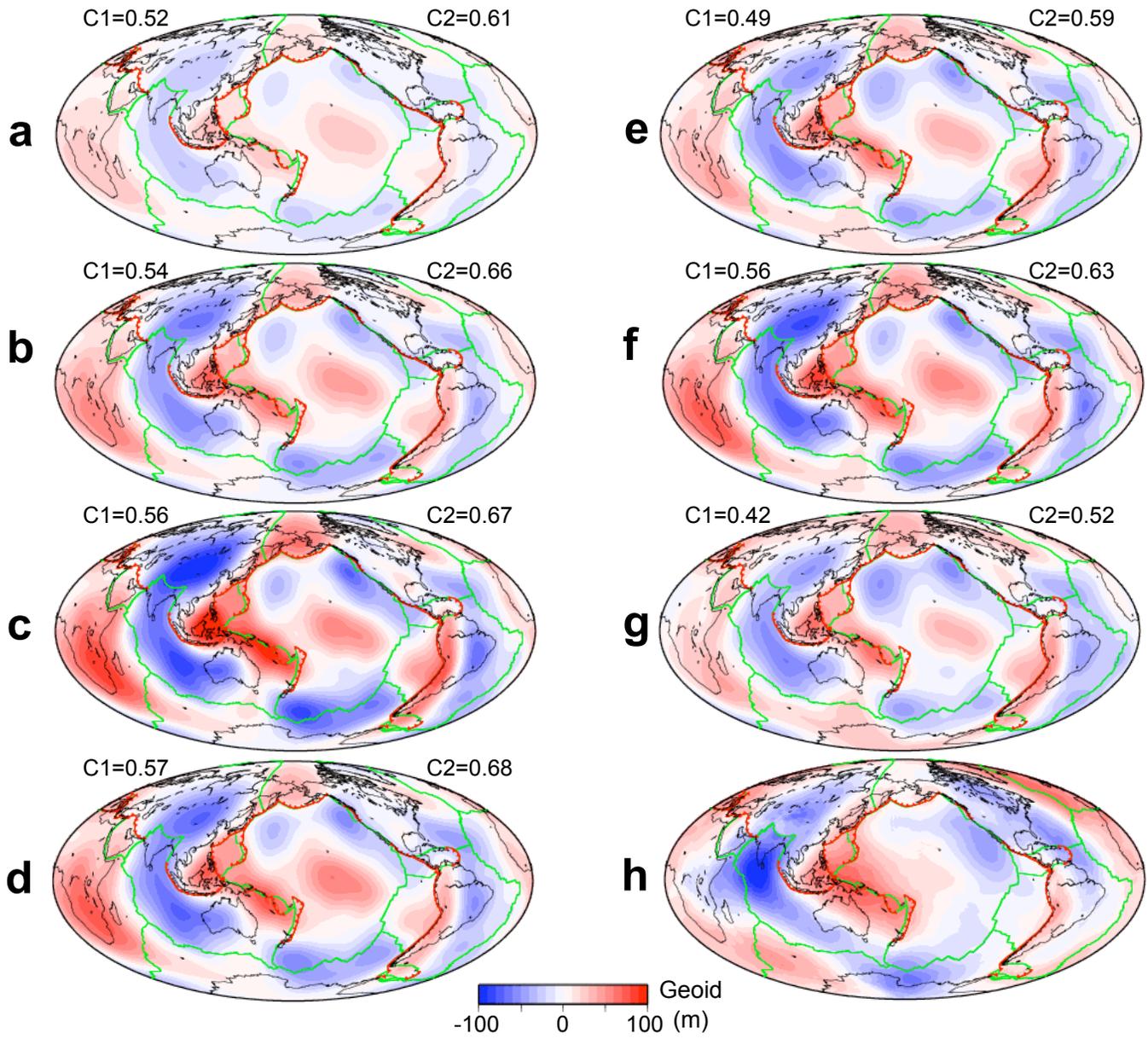
**Supplementary Figure S2**



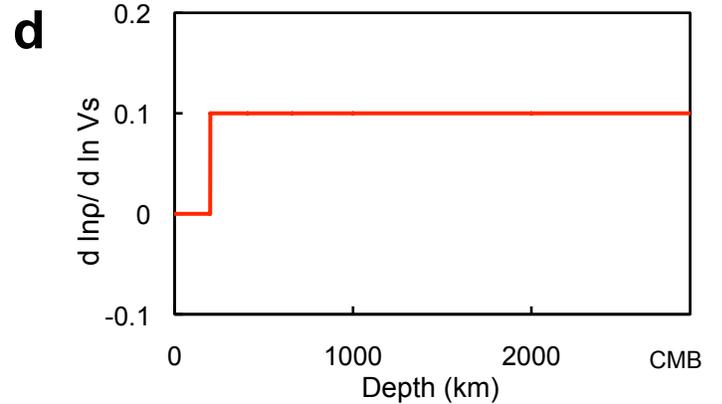
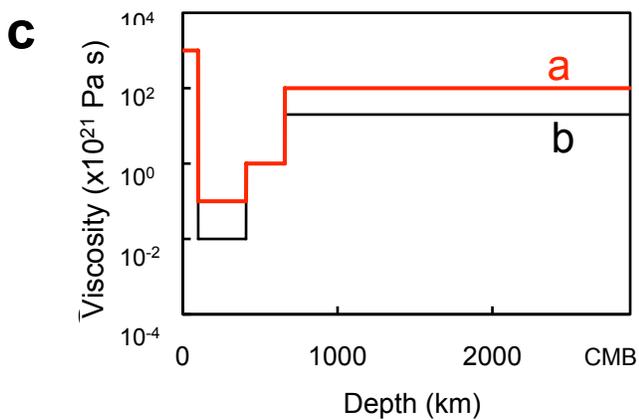
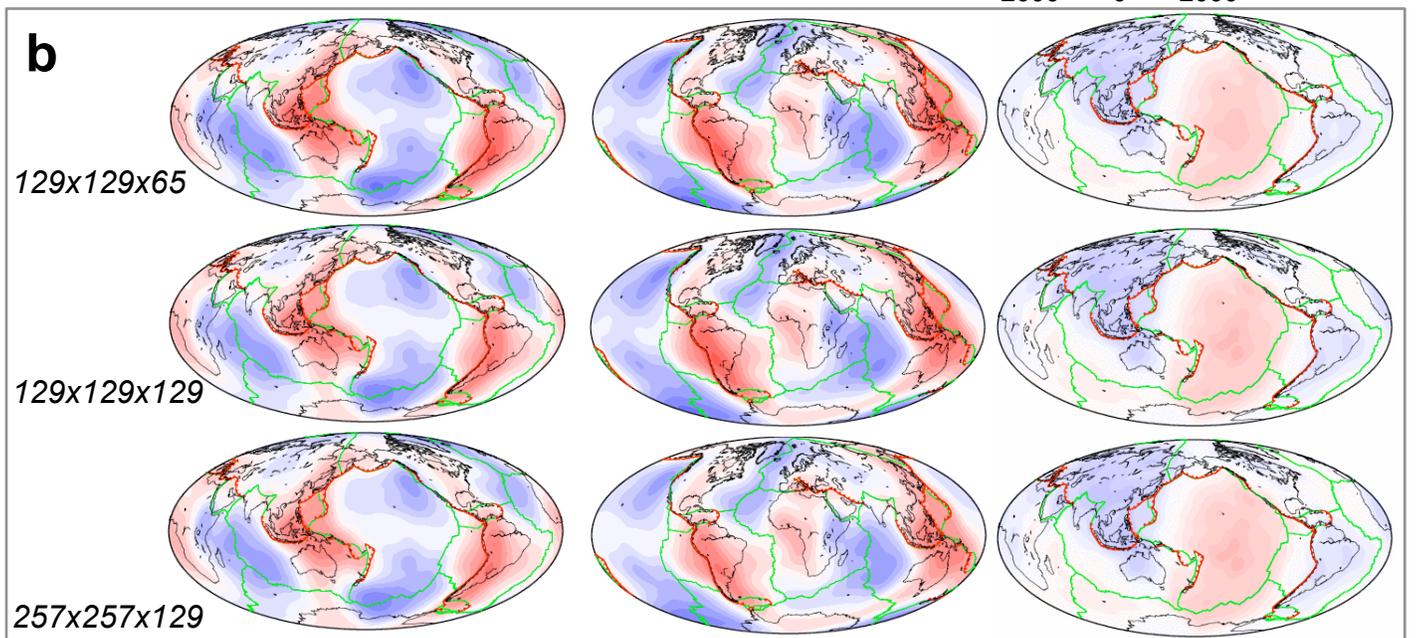
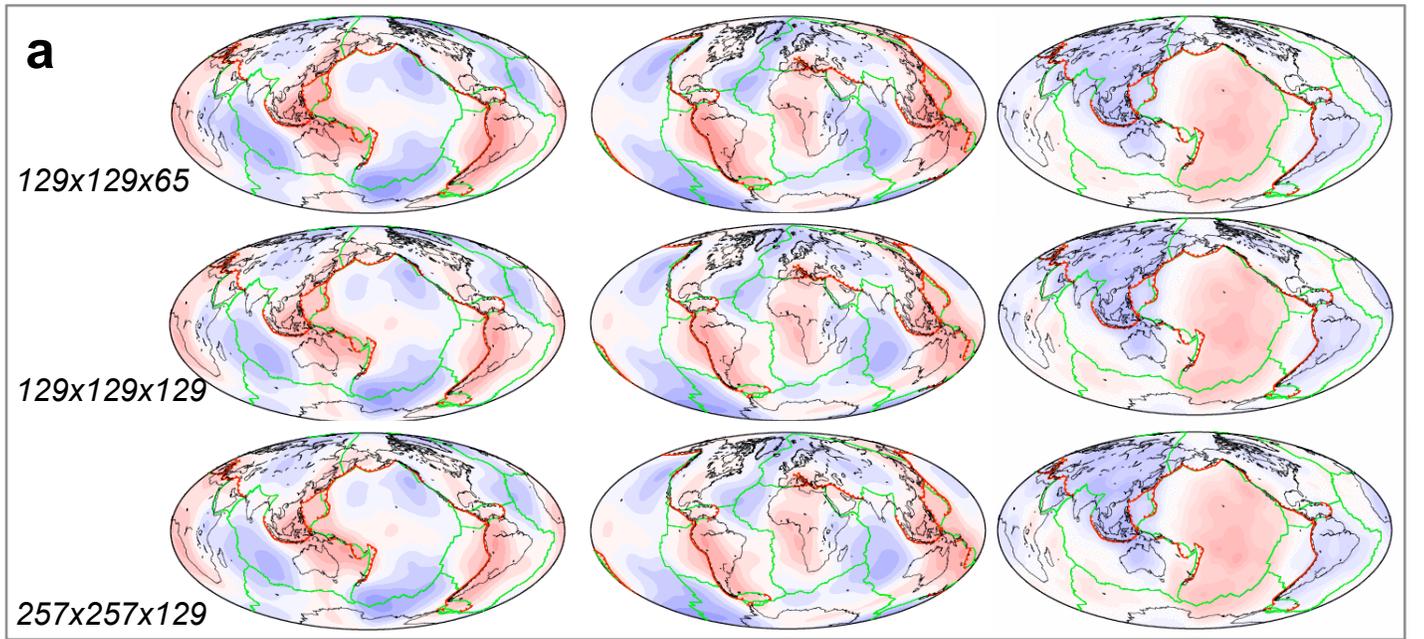
**Supplementary Figure S3**



**Supplementary**  
**Figure S4**



**Supplementary Figure S5**



**Supplementary Figure S6**