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Low loss polypropylene-silicon composites for **millimetre**wave applications

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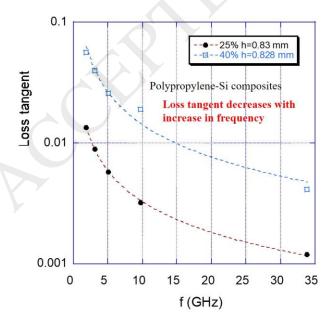
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Graphical abstract



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Highlights

All reported polymer-ceramic composites or hard ceramic substrates for microwave circuit applications show an increase in dielectric loss with increasing frequency in the microwave/millimetre frequency range. This is really problematic for high frequency applications such as IOT and 5G which are at very high frequencies. In the present paper we report for the first time the development of a composite (polypropylene-silicon) which shows a decrease in loss tangent with increasing frequency indicating the possibility of their use in 5G and Internet Of Things (IOT) as well as other high frequency or mm wave applications. This will lead to immense research on polymer-semiconductor composites for high frequency applications.

The results will be of great advantage in the future high frequency wireless communication and other applications.

Abstract

Polypropylene-silicon composite laminates were fabricated via hot pressing and their dielectric properties up to 35 GHz were studied. The loss tangent was found to decrease with increasing frequency whereas an increasing trend of loss tangent has previously been reported in the literature for such composites. The decreasing trend of the loss tangent with frequency is due to the decreasing conductor loss of silicon (Si)

and = indicates the possibility **for** use in high frequency applications such as **the** Internet Of Things and **5th** generation wireless communication. The composite containing 25 vol% of Si **had a** relative permittivity of 3.5 and **a** loss tangent of 0.001 at 35 GHz. The coefficient of thermal expansion and **the** thermal conductivity of 40 vol% Si loaded composites **were** 51 ppm/°C and 2.23 W/mK, respectively. The thermal conductivity of the composite increased by 163 % and 913 % for 25 and 40 vol% Si addition, respectively.

Key words: Millimetre wave materials, Microwave materials, Polymer-Silicon composites, Dielectrics, CTE, Thermal conductivity

1. Introduction

Materials with **a** low loss tangent and low relative permittivity (ε_r) are essential for **the** next generation **of millimetre**-wave communications. Recently, millimet**re**-wave wireless communication has begun to spread to public welfare systems in many countries. The frequency of millimet**re** wave communication ranges from 30 GHz (10 mm) to 300 GHz (1 mm). The wireless **gigabyte** (**WiGig**) **standard** (**IEEE 802.11ad**) for **millimetre**-wave wireless communication and vehicle radar **uses** 57 to 81 GHz. The WiGig **standard** has the highest data communication speed of 7 **Gbits** per second **over**

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short communication distances of approximately 10 m together with advanced properties such as security and power control. Presently, the microwave component industry uses several substrate materials comprised of both hard and soft substrates [1-5]. Hard substrates **are** usually α -alumina, magnesia, aluminum nitride, fused silica (quartz), cordierite, GaAs or beryllia. These ceramic (or quartz) substrates have the advantage of withstanding the localized heat generated during the wire-bonding process. Although hard substrates are highly isotropic, exhibit high thermal conductivity (k) and comparable CTE and can withstand very high operating temperatures, they suffer from brittleness, difficulty in machining and the relatively high cost of the chemically and thermally compatible conducting layer. Certain applications, such as patch antennas and base station circuitry, require substrates with larger sizes and consequently hard substrates are seldom used. In order to overcome these disadvantages, soft substrates based on ceramic filled thermoset plastic and thermoplastic have been developed [6,7]. These materials generally have good machinability, better shock resistance, low cost conduction/metallization layers, tailor-made properties and tight tolerances in their electrical properties. Furthermore, soft substrates based on some thermoplastic composites have more flexibility compared to thermoset based substrates. These are generally known as flexible substrates or

laminates. The size, shape, interfacial properties, percolation level and porosity of the filler particles have a crucial influence on the end properties of the composites [6,7]. Thermoplastic materials have a melt temperature associated with them, whereas the dimensional behavior of thermosets is characterized by their glass transition temperature (Tg). Generally, thermoset matrix composites are preferred for low end applications whereas thermoplastic composites are the choice of preference for high end microwave circuit applications. The main advantages of thermoplastic matrix composites compared to thermoset matrix composites are an unlimited shelf life, reprocessability, chemical inertness, lower moisture absorption, higher service temperature, high environmental tolerance and they do not require any curing [6,7]. However, the processing difficulties and relatively high melt viscosity are important **disadvantages** of thermoplastic materials. The recent explosive growth in the wireless market and advances in high speed digital technology have introduced new thermoset **and** thermoplastic materials with superior electrical performance to address these needs. More recently, butyl and silicone rubber filled with low loss ceramic have been reported for flexible electronic applications [8-11]. The ceramic based hard substrates and polymer or rubber filled with ceramic materials have suitable relative permittivity and loss tangent at **the** lower end of the microwave frequency regime [5].

However, as the frequency increases the loss tangent also increases although the relative permittivity is not much affected [2,5,6]. Consequently, these materials are unsuitable for millimetre wave or high frequency applications and there is an urgent need to find suitable polymer-ceramic composites with low loss tangents in the millimetre wave frequency regime. Silicon is reported as one of the most transparent materials for electromagnetic fields at high frequencies [12-14]. Float zone as-grown silicon has a relative permittivity of 11.6 and a loss tangent of about 10⁻⁴ (quality factor (Q) of 17800 at 49 GHz) [15]. The present paper reports the preparation, characterization and high frequency dielectric properties of polypropylene filled with silicon powder. Polypropylene is selected as the polymer matrix as it has a low loss tangent (10⁻⁴) with a relative permittivity of about 2.2 in the microwave/mm wave frequency region.

2. Materials and methods

In the present work, silicon from wafers grown by the float zone method was used as the particulate filler. The silicon wafers were crushed and powdered by ball milling using zirconia balls for about 12 hrs. The resultant silicon powder had a wide particle size distribution ranging from 10 to 100 μ m. Polypropylene (PP) powder and silicon filler were used as the starting materials for the preparation of the PP/ Silicon

composites. Commercial grade PP granules supplied by Reliance Industries Limited, India were used as the starting material. Fine PP powders were prepared by dissolving the PP granules in Xylene (95%, Merck) at a temperature of 130°C with continuous stirring from a magnetic stirrer. The dissolved material was taken out, dried, mixed with the Si powder and rigorously ground. The PP/Si composites were fabricated by compression molding using a hydraulic laminating press and a 125 mm x125 mm size stainless steel die set. The optimized pressure and temperature employed for hot pressing were 90 kg/cm² and 180°C for 20 minutes, respectively. Planar composite 125x125x1 mm laminates were obtained. The surface morphology and filler distribution in the composite samples were studied using a scanning electron microscope (Carl Zeiss, EVO 18 Research, UK). The low frequency measurements were made without any metalization, employing an Agilent Technologies 16451B Dielectric Test Fixture connected to a HP4294A precision impedance analyzer. The dielectric properties were measured in the microwave frequency range up to 35 GHz using different split Post Dielectric Resonators (SPDR) connected to an Agilent Technologies PNA-X vector network analyzer. The coefficient of thermal expansion of the samples was measured in the temperature range 30-120°C using an EXSTAR 6000 model thermo mechanical analyzer (SII Nano technology INC., Japan). The thermal

diffusivity and heat capacity were measured by laser flash analysis (LFA 427, Netzsch, Germany). The thermal **conductivity** (TC) was calculated using the data of thermal diffusivity, bulk density and heat capacity using the relation $TC=\alpha \times \rho \times Cp$ where α is the thermal diffusivity **and** ρ and Cp are **the bulk density and** specific heat capacity of the composites, **respectively**. The samples used had dimensions $10x10 \text{ mm}^2$ and thickness 1 mm and were carbon coated on both sides to enhance **the absorption of** laser flash light.

3. Results and Discussion

An SEM picture of a silicon wafer crushed using a mortar and pestle is shown in Fig. 1.

Ceramic particulates with a wide range of particle sizes from 10 to 130 µm are observed in the SEM picture.

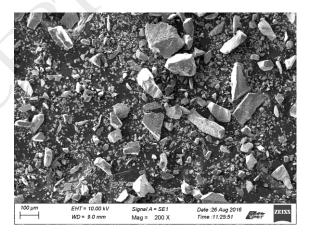


Fig. 1 SEM picture of powdered silicon **from** wafer

Silicon powders were incorporated in the PP matrix **by** fine mixing and compression molding techniques. 20, 25, 30, 35 and 40 vol % **samples** of PP/Silicon composites were prepared in the 125 mm x125mm stainless steel die. SEM pictures of **the** compression molded PP/Silicon samples are shown in Fig. 2.

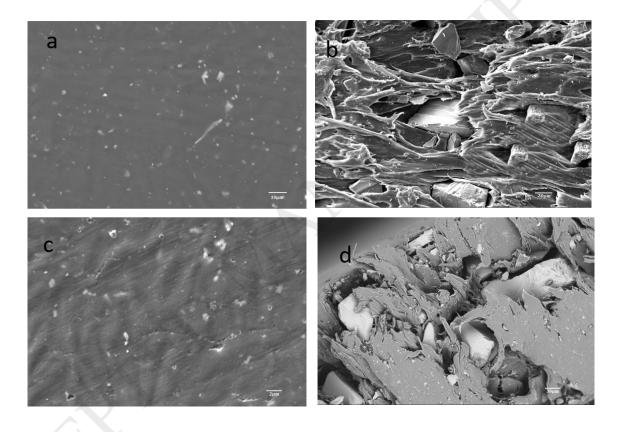


Fig. 2 (a) Planar and (b) cross sectional (fractured) micrographs of 30-vol % silicon filled PP **composite** (c) Planar and d) cross sectional (fractured) micrograph of 40 vol% silicon filled **PP composite**

It is evident from the planar microstructure (Fig 2(a)) of the 30 vol % silicon filled PP composite that the ceramic particulates **were** uniformly distributed in the polymer

matrix with a nearly **pore-free** microstructure. The cross sectional **pictures also show a** fine distribution of Si particles with varying sizes. As the volume fraction of Si increased in the PP matrix, porosity **started to appear** in the composite. **This** is clearly evident from the planar microscopic image of the 40 vol % Si filled PP **composite** (Fig. 2(c)).

Low frequency measurements **were** performed using an impedance analyser and capacitive dielectric test fixture. In the capacitive measurements the sample under test **was** inserted between the two electrodes of an air capacitor and, together with the air gap above, the sample **created** a double-layer capacitor. **A schematic** of **the** capacitive measurement cell used in the experiments is show in Fig.3.

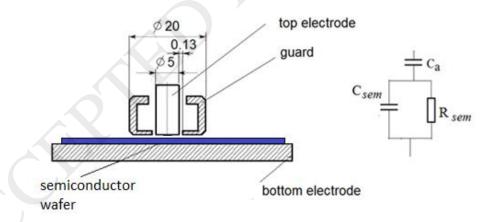


Fig.3. Agilent Technologies 16451B Dielectric Test Fixture with **5 mm diameter** guarded electrode **that was** used in the **experiments**.

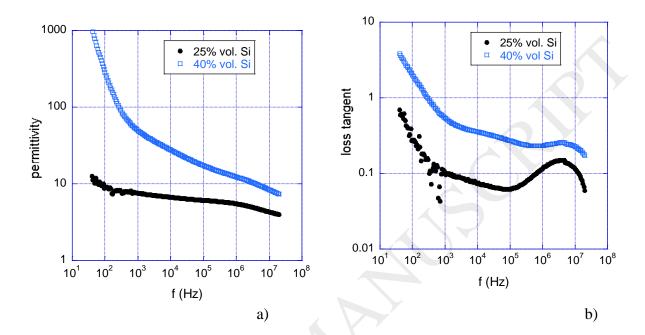


Fig.4. Variation of (a) relative permittivity and (b) loss tangent as a function of frequency up to 15 MHz (low frequency measurements).

The dielectric properties of two representative samples 25 and 40 vol% are shown in Fig. 4. The relative permittivity of the composites showed a decreasing trend with respect to frequency up to 15 MHz. The change in relative permittivity was more for the 40 vol% composite as compared to 25 vol% silicon filled samples. This could be due to the space charge contribution from the greater amount of interface region in the 40 vol% filled samples. This was further evident from the frequency versus loss tangent graph.

As the frequency increased, the dispersion in the relative permittivity also **showed** a decreasing trend. The loss tangent also **showed** a linear decrease with respect to frequency with a relaxation peak around 10^6 - 10^7 .

The frequency dependence of relative permittivity and loss tangent measured at high frequencies on two samples is shown in Fig. 5. These experiments were performed using five SPDR's having nominal frequencies of 1.9 GHz, 3.1 GHz, 5 GHz, 10 GHz and 35 GHz. It was seen that the loss tangent was governed by conductor losses in the silicon particles. It is expected that at higher frequencies losses will be much lower.

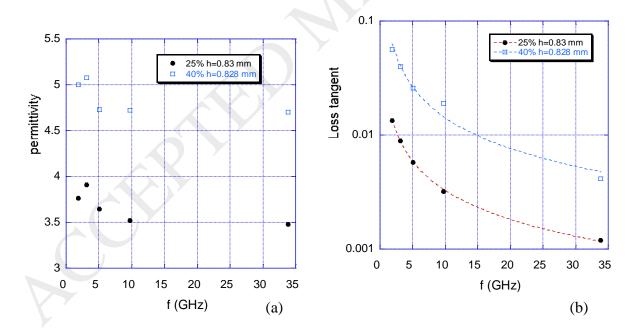


Fig.5. (a) Relative permittivity and (b) dielectric loss tangent of PP-Si samples at frequencies up to 35 GHz

The relative permittivity of the composite samples remained more or less constant from 10 GHz to 35 GHz (Fig. 5). Interestingly, the loss tangent of the composites exhibited a sharp decrease with respect to an increase in frequency. It is inferred that such a variation is mainly due to the relatively lower loss tangent of the Si particulates at higher frequencies. The as-grown float zone silicon had a resistivity of about 80 $k\Omega$.cm. The loss tangent of a material includes losses due to intrinsic and extrinsic factors and it is also affected by the conductivity of the material (conductor loss). The conductor loss decreases as the frequency increases [16]. It is well established that the loss tangent in silicon decreases with increase in frequency [14-18] due to a reduction of the conductor losses. Fig. 6 shows the variation of resonant frequency shift and loss tangent of PP-25% Si composite as a function of temperature in the range 23-123 °C measured using an SPDR operating at 4.8 GHz. It gives the temperature coefficient of permittivity to be about -21 ppm/°C. It should be noted that the relative resonance frequency shift variations of the SPDR shown in Fig.6a were similar to the relative permittivity variations of the sample. This is quite different from the case of measurements of bulk samples acting as dielectric resonators. The loss tangent of the composite increases with increase in temperature and was due to the increase of the effective conductivity inside the Si particles.

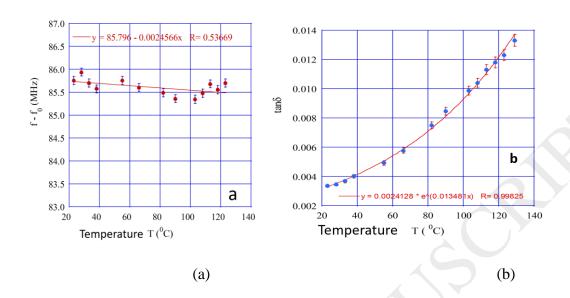


Fig. 6. Variation of (a) resonant frequency shift and (b) loss tangent of PP-25%Si composite measured as a function of temperature using **an** SPDR operating at 4.8 GHz.

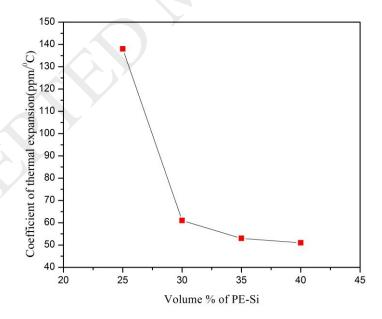


Fig. 7. Coefficient of thermal expansion of PP-Si samples with varying vol%

Si

Figure 7 shows the variation of CTE of the composite samples as a function of the volume fraction of Si loading. **A** decrease in CTE **was** noticed as a result of filler loading in the PP matrix. **A** CTE of 51 ppm/°C **was** obtained for 40 vol% Si filled PP composites.

The thermal conductivity is also an important parameter for microelectronic applications. The heat transfer in a material is related to thermal conductivity, diffusivity and specific heat capacity. A low thermal conductivity value is generally preferred for minimizing heat losses in applications but a high thermal conductivity is required to dissipate heat generated in a device or when heat needs to transfer from one site to another. In the PP-Si composites, the thermal diffusivity slightly decreased with increase in temperature as shown in Fig. 8. The decrease was significant for the more heavily Si loaded samples because Si is a metalloid. The increase in specific heat of the composites with increase in temperature is shown in Fig. 9.

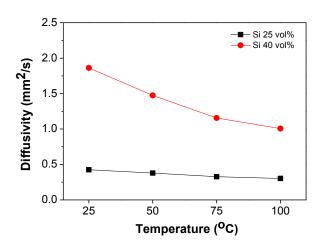


Fig.8. Variation of thermal diffusivity as a function of temperature

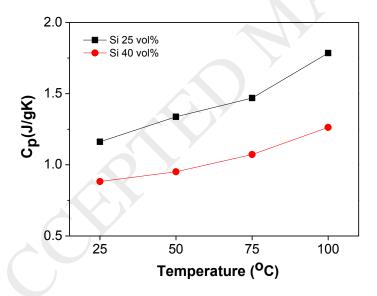


Fig. 9 Variation of specific heat as a function of temperature

Figure 10. shows the variation of thermal conductivity of the composites as a function of temperature. At room temperature (25°C), the PP-25 vol% Si composite had

a thermal conductivity of 0.58 W/mK and the PP-40 vol% Si had 2.23 W/mK. The thermal conductivity **remained** nearly constant for the pp-25 vol% Si composite but it decreased significantly for the PP-40 vol% Si composite with an increase in temperature up to 100°C. The PP-25 vol% Si had an experimental density of 1.152 g/cm³ and that of PP-40 vol% Si was 1.358 g/cm³. In general, PP has a low thermal conductivity of about 0.22 W/mK whereas the Si has a high thermal conductivity of about 150 W/mK. The thermal conductivity increased to only about 0.58 W/mK for the composite with 25 vol% whereas it increased to 2.23 WmK when the Si content was increased to 40 vol%. The increase in thermal conductivity was relatively low considering the high thermal conductivity of Si. This is due to the fact that there is poor connectivity between the thermally conducting Si particles in the composite below the percolation threshold and the resultant properties depend on the PP matrix. However, it may be noted that the thermal conductivity of the PP composite increased by 163 % and 913 % for 25 and 40 vol% Si addition, respectively. It is clear from the present study that the thermal conductivity of pristine PP (0.22 (W/mK) can be considerably improved by the addition of silicon.

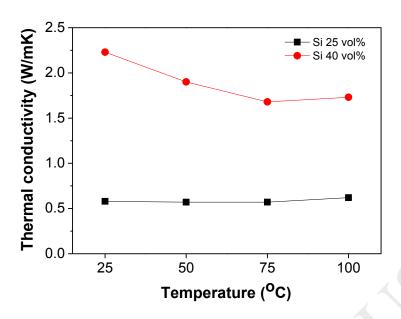


Fig. 10 Variation of thermal conductivity as a function of temperature

There are many factors, such as temperature, density, porosity, moisture, degree of crystallinity, orientation of grains, size of molecules **and** impurities, which can affect the thermal conductivity of a material [19,20]. The composite containing 40 vol% Si had higher porosity as evidenced by the SEM pictures shown in Fig.2. It **has been** reported that the thermal conductivity (k) of polypropylene exhibits a smooth decrease with increase in temperature from 0.25 to 0.15 in the temperature range 25 to 100°C [19]. This behavior was attributed in terms of two mechanisms **with opposing** effects [19]: the specific heat increases slightly when the temperature rises, but the thermal diffusivity reduces due to the decrease in the phonon mean free path. The reduction in

the polymer density (bulk density) with temperature also contributes to the reduction in thermal conductivity. The net effect of these mechanisms is a smooth decrease of the thermal conductivity with respect to a rise in temperature. The thermal conductivity of any material is dependent on two things: (a) the motion of free electrons (b) lattice vibrations [19,20]. In metals, the thermal conductivity is mainly dependent on the motion of free electrons. The molecular vibrations increase with an increase in temperature and thus increase the mean free path of **the molecules, hence** obstructing the flow of free electrons. This **reduces** the thermal conductivity. The heat conductivity in non-metals is mainly due to phonons (lattice vibrations). Hence the thermal conductivity of non-metals is nearly a constant at low temperatures.

The PP-Si composite **had a** suitable relative permittivity, a low loss tangent which decreased with increasing frequency and a relatively high thermal conductivity. Such flexible composite laminates are ideal candidates for IOT and 5G applications. It has recently **been** reported that high energy proton irradiated Si can have a high resistivity and is highly transparent to electromagnetic waves at frequencies up to far infrared frequencies [12,13]. The increase in resistivity is due to the formation of both shallow and deep radiation defect centers that are responsible for the charge compensation in the material [21]. This high resistivity silicon has a high quality **factor** (low loss tangent) in

the **millimetre** wave frequency range [14,15,17] and **the use of such** high resistivity Si may further improve the loss tangent **in the composites.**

4. Conclusion

Composites of polypropylene containing 25 and 40 vol % Silicon were fabricated by compression molding using a hydraulic laminating press. The CTE of the composites decreased with increasing amounts of silicon. The thermal conductivity was improved by the addition of silicon. The composite containing 40 vol% Si had a relative permittivity of 4.1, a loss tangent of 0.006 at 35 GHz, a CTE of 51 ppm/°C and a thermal conductivity of 2.23 W/mK. The microwave dielectric properties and thermal properties could be tailored by changing the Si content in the PP matrix. The relative permittivity remained nearly constant but the loss tangent decreased with increasing frequency. These results show that the loss tangent of PP-Si composites decreases as a function frequency whereas other PP-composites reported in the literature show an increase in loss tangent with increasing frequency. This decreasing tendency of loss tangent with increase in frequency indicates the possibility of the use of these polypropylene composites in microwave and millimetre wave communication systems. In addition, they are important candidate materials for the Internet of Things (IOT) and 5G applications.

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Figure captions

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