# Quantitative Models in Marketing Research: Corrections and Additions\*

Philip Hans Franses

Econometric Institute

Marketing and Organization

Erasmus University Rotterdam

and

Richard Paap

Econometric Institute

Erasmus University Rotterdam

December 11, 2007

#### Chapter 2

- Page 22, 11th line from above: Replace "10–20 guilders" by "0–20 guilders".
- Page 25, 14th line from above: Replace "25–50 days" by "0–50 days".
- Page 26, Table 2.6, Notes a,b,c: Replace "the brand" by "liquid detergent".

### Chapter 3

• Page 34, equation (3.13): The correct equation is

$$\frac{\partial \sum_{t=1}^{T} (y_t - X_t \beta)^2}{\partial \beta} = -2 \sum_{t=1}^{T} X_t'(y_t - X_t \beta) = 0.$$

<sup>\*</sup>Book published by Cambridge University Press 2001. We thank Sven Dijkshoorn, Dennis Fok, Petra Halferkamps, Carter Hill, Martijn de Jong, Kar Yin Lam, Agatha Schouten, Marjolein van Baardwijk, Erjen van Nierop, Björn Vroomen, and students of the Marketing Models 1 course at the Erasmus University Rotterdam for their contributions.

• Page 37, equation (3.24): Divide  $\hat{\mathcal{I}}$  by T. The correct equation is

$$\sqrt{T}(\hat{\theta} - \theta) \stackrel{a}{\sim} N(0, (\hat{\mathcal{I}}/T)^{-1}).$$

• Page 38, first line of equation (3.28). The correct equation is

$$\frac{\partial l(\beta, \sigma^2)}{\partial \beta} = -2 \sum_{t=1}^{T} \frac{1}{\sigma^2} X'_t(y_t - X_t \beta) = 0.$$

• Page 53, equation (4.11): Replace  $\varepsilon_{A,i} - \varepsilon_{B,i}$  by  $\varepsilon_{B,i} - \varepsilon_{A,i}$ .

#### Chapter 4

- Page 54, equation (4.12): Add the following sentence after the equation: where we use in the final line of the equation the assumption that the distribution of  $\varepsilon_i$  is symmetric.
- Page 56, equation (4.17): Left parenthesis is missing in the final line of the equation. The correct equation (4.17) is:

$$= \frac{\exp\left(\beta_1(\frac{\beta_0}{\beta_1} + x_i)\right)}{1 + \exp\left(\beta_1(\frac{\beta_0}{\beta_1} + x_i)\right)}$$

• Page 60, equation (4.40): This equation shows minus the expected value of the Hessian matrix (information matrix) instead of the Hessian matrix. The correct text has to be: ... and the expected value of the Hessian is given by

$$E[H(\beta)] = E\left[\frac{\partial^2 l(\beta)}{\partial \beta \partial \beta'}\right] = -\sum_{i=1}^N \frac{\phi(X_i \beta)^2}{\Phi(X_i \beta)(1 - \Phi(X_i \beta))} X_i' X_i.$$

The asymptotic covariance matrix of the parameters  $\beta$  can be estimated by  $(-E[H(\beta)])^{-1}$ , evaluated in the ML estimate  $\hat{\beta}$ .

- Page 63, below equation (4.49): Simulations in Davidson & MacKinnon (1984, *Journal of Econometrics*) show that the best statistic to use in finite samples is the explained sum of squares from regression (4.49). This test statistic is also used in the application in Section 4.4.
- Page 64, 1st line below equation (4.53): Replace "Notice that the lower bound ... equal to zero." by "The lower bound value of this  $R^2$  is equal to 0. The upper bound is however only equal to 1 when  $\Pr[Y_i = y_i | X_i] = 1$  for all i which will hardly happen in practical situations.".
- Page 74, 2nd line below equation (4.74): Remove "log". The correct sentence is: For the Logit model, one can easily find the link between  $\Pr_s[Y_i = 1]$  and  $\Pr_p[Y_i = 1]$  because this model holds that the odds ratio is ...

#### Chapter 5

• Page 80, equation (5.9): The second  $x_i$  variable in the numerator has to be inside parentheses. The correct equation is:

$$\frac{\partial \Pr[Y_i = j | X_i]}{\partial x_i} = \frac{(1 + \sum_{l=1}^{J-1} \exp(\beta_{0,l} + \beta_{1,l} x_i)) \exp(\beta_{0,j} + \beta_{1,j} \mathbf{x_i}) \beta_{1,j}}{(1 + \sum_{l=1}^{J-1} \exp(\beta_{0,l} + \beta_{1,l} x_i))^2} - \frac{\exp(\beta_{0,j} + \beta_{1,j} x_i) \sum_{l=1}^{J-1} \exp(\beta_{0,l} + \beta_{1,l} x_i) \beta_{1,l}}{(1 + \sum_{l=1}^{J-1} \exp(\beta_{0,l} + \beta_{1,l} x_i))^2}$$

• Page 84, equation (5.25): Remove

and 
$$\sum_{l=1}^{J} \frac{\partial \Pr[Y_i = j | w_i]}{\partial w_{i,l}} w_{i,l} = 0.$$

This equality is not true.

- Page 87, equation (5.29): The term  $du_{i,j}$  has to be at the end. The correct equation is  $\int_{0}^{\infty} \int_{0}^{u_{i,j}} \cdots \int_{0}^{u_{i,j}} f(u_{i,1}, \ldots, u_{i,J}) du_{i,1} \ldots du_{i,j-1} du_{i,j+1} \ldots du_{i,J} du_{i,j}$
- Page 87, equation (5.30): The term  $\exp(-\varepsilon_{i,j})$  is missing. The correct equation is

$$f(\varepsilon_{i,j}) = \exp(-\varepsilon_{i,j}) \exp(-\exp(-\varepsilon_{i,j})), \text{ for } j = 1, \dots, J,$$

- Page 99, 3rd line below equation (5.64): Replace "because  $\ell(\hat{\theta})$  will never be 0." by "because  $\ell(\hat{\theta})$  will never be 0 in practical situations."
- Page 102, 19th line from above: Replace 32.98 by 45.51.
- Page 104, 11th line from above: Replace "0.025 and 0.050" by "-0.46 and -0.40".
- Page 104, 6th line from below: Replace "-0.46 and -0.40" by "0.012 and 0.055".
- Page 110, 7-8th line from above: Correct notation is
   'Specify log-likelihood for Multinomial Logit model logl mnl
- Page 110, 14th line from above: exp(xb4) has to be exp(xb1). The correct line is: mnl.append denom=1+exp(xb1)+exp(xb2)+exp(xb3)

#### Chapter 7

- Page 140, 8th line from below: Replace "donates" by "does not donate". The correct sentence is: The probability that an individual does not donate to charity is now given by ...
- Page 143, 7th line from below: Replace  $\hat{\beta} = \hat{\gamma}\hat{\xi}$  by  $\hat{\beta} = \hat{\gamma}/\hat{\xi}$ .
- Page 145, equation (7.33): Replace  $I[y_i = 1]$  by  $I[y_i > 0]$ .
- Page 146, equation (7.35): Replace  $\Phi(-X_i\alpha)$  by  $\log(\Phi(-X_i\alpha))$ . Likewise, replace  $(1 \Phi(-(X_i\alpha + \sigma_{12}\sigma_2^{-2}(y_i X_i\beta))/\tilde{\sigma})$  by  $\log(1 \Phi(-(X_i\alpha + \sigma_{12}\sigma_2^{-2}(y_i X_i\beta))/\tilde{\sigma})$ .
- Page 146, equation (7.35): Replace  $I[y_i = 1]$  by  $I[y_i > 0]$  (2 times).
- Page 154, 19th line from below: Replace 14.36 by 14.61.

#### Chapter 8

- Page 159, 7th line from below: Replace [0,1] by (0,1). The correct sentence is: ... maps the explanatory variable  $x_i$  on the unit interval (0,1) (see also Section 4.1).
- Page 167, 4th line from above: Replace  $\gamma = 1$  with  $\gamma = 1$ .
- Page 171, equation (8.47): Replace a by  $\alpha$ . The correct equation is given by

$$\frac{\partial \Lambda_0(t_i)}{\partial \alpha} = t^{\alpha} \log(t) \qquad \frac{\partial^2 \Lambda_0(t_i)}{\partial \alpha^2} = t^{\alpha} (\log(t))^2.$$

• Page 172, equation (8.50): The third line of this equation has to be

$$1 - S(\Lambda^{-1}(E|X_i))$$

- Page 175, 13th line from above: Replace a by  $\alpha$  in the expectation. The correct senctence is: For the Proportional Hazard specification, the expectation equals  $\exp(-X_i\beta)^{1/\alpha}\Gamma(1+1/\alpha)$ .
- Page 175, 2nd line of equation (8.61): Replace T by  $T_i$  in the denominator. The correct formulation is:

$$=1-\frac{\Pr[T_i > t + \Delta t | X_i]}{\Pr[T_i > t | X_i]}$$

- Page 177, Table 8.3: Estimate of scale parameter  $\gamma$  has to be 0.019 instead of -0.019.
- Page 178, 3rd line from below: Replace longer by shorter.

• Page 179, equation (8.66): Delete the log operator in the numerator of the second equation. The correct formulation of (8.66) is

$$f(t_i|X_i, v_i) = -\frac{dS(t_i|X_i, v_i)}{dt_i}$$

• Page 183, 3rd line of Section 8.A.2: Add coef(8) b = 1.

# **Appendix**

• Table A.3, line *Normal distribution*. In the column pdf the term  $\sigma^{-1}$  is missing. It should read

 $\frac{1}{\sigma} \frac{1}{\sqrt{2\pi}} e^{-\frac{(y-\mu)^2}{2\sigma^2}}$ 

• Notes of Table A.3, 2nd line from below:  $1/\sigma((y-\mu)/\sigma)$  has to be  $1/\sigma\phi((y-\mu)/\sigma)$ .

## **Bibliography**

- Page 196: correct pages for Amemiya, T. (1981) are 1483–1536.
- Page 198: correct volume number and pages of the Hausman, J.A. and D. Wise (1978) reference are *Econometrica*, **46**, 403–426.

# Subject Index

- Page 204: elasticity, Linear Regression model, 32–33
- Page 206: White standard errors, 146