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## **Economic Evaluations in Exploration**

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Friedrich-Wilhelm Wellmer  
Manfred Dalheimer  
Markus Wagner

# Economic Evaluations in Exploration

Second Edition

With 68 Figures and 61 Tables



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Cover: The boundary between ore and waste = cut-off boundary see Sect. 10.1

Craig Nickel-Copper Mine, Falconbridge Sudbury, Canada

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*To Helgard and Georg,  
who asked if I was writing a book about bear hugs*

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## Preface to the Second Edition

This textbook, now in its second English edition, is originally a translation of the German textbook “Rechnen für Lagerstättenkundler und Rohstoffwirtschaftler, Teil 1”, also translated into the Chinese and Russian languages. Compared to the previous English and German editions the chapters have been updated with new examples and in many cases amended.

The textbook is intended for the economic geologist who deals with the evaluation of deposits at an early stage of development. Once an exploration project has reached the feasibility stage, the exact calculations that are necessary for a comprehensive technical and economic assessment will be performed by a team of geologists, mining engineers, metallurgists, and economists. In the early stages of exploration, however, any evaluator of deposits must be able to cover the whole spectrum himself.

Since only order of magnitude parameters are available at this early stage, the calculations can only yield order of magnitude results. Precise calculations would even be misleading, since the evaluation does not yet aim at accurate economic assessment but at making the right decision: should the investigation be abandoned or should it be continued at higher costs and with more detailed methods.

Therefore, this textbook offers rules for quick and easy calculations based on the application of approximate data. It hopes to provide both the student and the geologist in the field with a complete set of rules and methods enabling to perform a quick initial evaluation of the deposit without the support of specialists or computers – even if he is left to his own resources. To support the “how to do”-approach all rules for calculations are illustrated with examples. The textbook also points out mistakes and pitfalls the authors encountered when working for the exploration industry or gave seminars.

In addition, it is intended as a compendium. Every calculation can be done by hand or by a calculator. Since cost data vary from country to country, absolute figures are only given as examples, but advice is offered on how to adjust the available data to any particular case.

Ultimately, these calculations do little more than transform initial geological data, like reserves and grades, into a simple economic model that can then be used to decide, before committing further funds to the venture, whether an occurrence of mineralization has, or does not have, the promise of economic viability. This transformation of preliminary geological data into the final economic model is merely a routine mechanical procedure. Of importance is the quality of input which depends on the correct initial geological evaluation of tonnage and grades, reserves and potential! Therefore quality control in sampling and analytical procedures is a crucial aspect in the eval-

ation of any exploration or mining project right from the start. This aspect is dealt with in the book Wellmer 1998 (Statistical Evaluation in Exploration for Mineral Deposits).

For a project evaluation frequently a geologist has to research data quickly. Here the internet is an invaluable tool. To help to find relevant data quickly often internet addresses are given in the text. In addition in Appendix F relevant possible sources of information with internet addresses are listed.

We should like to acknowledge our appreciation to B. Bognar, Friedberg, Germany and S. Schmidt, Cardiff, UK, who critically read the manuscript and made numerous suggestions for improvements including the spread sheet for density calculations in Appendix C, but shortcomings are, of course, the responsibility of the authors. We also thank E. Gschwindt, Luxembourg, M. Glasson, Perth, Australia, K.-H. Huck, Wolfach, Germany, P. L. Nelles, Bensheim, Germany, S. Schmidt, Cardiff, UK, and A. Schneider, Santiago, Chile, for support in up-dating the rules-of-thumb for interest rates and operating and capital costs, F. Barthel and H. Kaiser for information related to uranium, P. Buchholz, Hannover, Germany for research on various topics, U. and F. Dennert, Hannover for advice on probabilities, E. von der Linden, Dreieich, Germany, for advice on concentrate grades, W. Loer, Essen, Germany for uranium energy conversion factors, K. Stedingk, Halle, Germany, for the information of massive ore shoot grade control in the Grund mine, Germany and Mrs. B. Ogiolda, D. Lohmann and M. Zachcial, Bremen, Germany for information of sea freight rates. For technical support our special thanks are due to Mrs. D. Homberg, Mrs. M. Simon and Mrs. E. Westphale, Hannover.

*Friedrich-Wilhelm Wellmer*

*Manfred Dalheimer*

*Markus Wagner*

Hannover, October 2007

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## Preface to the First Edition

This textbook is a translation of the German textbook “Rechnen für Lagerstättenkundler und Rohstoffwirtschaftler, Teil 1” published by the Ellen Pilger Publishing Company. Those passages in the German edition which were especially written for the German readership were transformed for English speaking readers. Compared with the German edition many chapters have been slightly amended. The main new additions in this English version are the chapter on linear optimization in Chapter 10.2 and Chapter 12 on the comparison of ore deposits.

The textbook is intended for the economic geologist who deals with the evaluation of deposits at an early stage of development. Once an exploration project has reached the feasibility stage, the exact calculations of the deposit, the technical and economic assessment will be performed by a team of geologists, mining engineers, metallurgists, and economists. In the early stages of exploration, however, any evaluator of deposits has to be able to cover the whole spectrum himself.

Since only order of magnitude parameters are available at this stage, the calculations can only yield order of magnitude results. Precise calculations would even be misleading, since the evaluation does not yet aim at accurate economic assessment but at making the right decision: should the investigation be abandoned or should it be continued at higher costs and with more detailed methods.

Therefore, this textbook offers rules for quick and easy calculations based on the application of approximate figures. It hopes to provide both the student and the geologist in the field with a complete set of rules and methods enabling him to perform a quick initial evaluation of the deposit without the support of specialists or computers – even if he is left to his own resources.

In addition, it is intended as a compendium. Every calculation can be done by hand or by calculator. Since cost data vary from country to country absolute figures are only given as examples, but advice is given on how to adjust the available data to any particular case.

Ultimately, these calculations do nothing but transform initial geological data like reserves and grades into an economic unit and decide if an occurrence of mineralisation can be regarded as an economically viable ore deposit. This transformation of preliminary geological data into the final economic unit is merely a routine mechanical procedure. Of importance is the quality of input which depends on the correct initial geological evaluation of tonnage and grades, reserves and potential!

I should like to acknowledge my appreciation to Dres. Bering (Hannover), Gschwindt (Bong Mine, Liberia), Kaiser (Erlangen), Kollwenz (Frankfurt), Sommerlatte (Zug) and Thalenhorst (Toronto) for initially reading the manuscript and making numerous suggestions for improvements, to G. Kater (Sydney) who supplied the niobium-tantalum data in Chapter 5.2., and to Dr. Heide (Meggen) for the advise on the Bond index. My special thanks are due to Mrs. U. Grawe (Melbourne) and Mr. B. Bognar (Frankfurt) for translating the German text into English.

Hannover, Spring 1989

FRIEDRICH-WILHELM WELLMER

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# Contents

<b>Introduction .....</b>	<b>1</b>
<b>1   Conversions .....</b>	<b>3</b>
1.1 Conversion of Units .....	5
1.1.1 Measures of Length .....	5
1.1.2 Square Measures .....	6
1.1.3 Cubic Measures/Dry Measures .....	6
1.1.4 Mass Units .....	7
1.1.5 Other Units .....	10
1.2 Conversion of Derived Quantities .....	12
1.2.1 Map Scales (on the Basis of Mile, Chain, Feet) .....	12
1.2.2 Density Conversions .....	13
1.2.3 Grades .....	15
1.2.4 Accumulation Values/Intensity Factors .....	17
1.2.5 Production .....	17
1.2.6 Waste to Ore Ratios .....	18
1.2.7 Specific Metal Prices .....	18
1.3 Conversion of Chemical Compounds .....	19
<b>2   First Estimates of Grade and Tonnages and Potential Grade and Tonnages .....</b>	<b>21</b>
2.1 Estimation of Volume and Tonnage of Ore Deposits .....	22
2.1.1 Calculating the True Thickness .....	22
2.1.2 Reserve Estimations Based on Sections .....	27
2.1.3 Reserve Estimations on the Basis of Plan Maps .....	28
2.2 Grade Estimation and Weighting .....	29
2.2.1 Weighting in Reserve Calculations .....	29
2.2.2 Grade Calculations for Massive Ore Shoots .....	32
2.2.3 Grade Determinations from Geophysical Downhole Logging .....	34
2.2.4 Grade Determination from Coverage Data Per Unit Area .....	38
<b>3   Dealing with Data of Multi-Element Deposits .....</b>	<b>41</b>
3.1 Metal Ratios .....	41
3.2 Ternary Diagrams .....	42
3.3 Regression Analysis .....	43
3.4 Standardizations .....	48

3.5	Calculating Metal and Value Equivalents .....	50
3.5.1	Introduction .....	50
3.5.2	Calculating Metal Equivalents .....	50
3.5.3	Calculating Density Equivalents .....	52
<b>4</b>	<b>Conversion of Geological Data into Mining Data for Ore Deposits .....</b>	<b>55</b>
4.1	Dilution .....	55
4.2	Mining Recovery of Tonnages or Loss of Tonnages Respectively .....	56
4.3	Metal Recovery in the Beneficiation Plant .....	56
4.4	Concentration Factor and Mass Recovery .....	58
4.5	Special Case Uranium .....	58
<b>5</b>	<b>Introduction to Economic Evaluations .....</b>	<b>61</b>
<b>6</b>	<b>Metal Prices .....</b>	<b>63</b>
6.1	Introduction .....	63
6.2	Choice of Currency .....	63
6.3	Calculation of Average Prices Adjusted for Inflation .....	65
6.3.1	Introduction .....	65
6.3.2	Correcting Prices for Inflation Effects .....	66
6.4	Calculating Prices with Moving Averages .....	67
6.5	Deriving Prices from Cost Charts .....	68
<b>7</b>	<b>Calculation of the Net Smelter Return (NSR) of a Mine .....</b>	<b>71</b>
7.1	Simple Cases on the Basis of Prices Per Unit or Direct Concentrate Prices .....	71
7.2	Non-Ferrous Metals .....	72
7.2.1	Calculating with Smelter Formulae .....	72
7.2.2	Calculating with Rules-of-Thumb .....	74
<b>8</b>	<b>Production Lifetime .....</b>	<b>79</b>
8.1	Rules-of-Thumb for the Lifetime of Deposits .....	79
8.1.1	General Rules .....	79
8.1.2	Rules Based on Mining Experience .....	79
8.1.3	Calculating the Optimal Lifetime .....	80
8.2	Market Barriers as a Determinant for a Mine Capacity .....	83
8.3	Lifetime Considerations in the Construction Minerals Industry .....	84
8.4	Ratio of Lifetime of Reserves .....	84
<b>9</b>	<b>Calculation of Cost Data .....</b>	<b>87</b>
9.1	Provision of Cost Data .....	87
9.1.1	Collection of Cost Data .....	87
9.1.2	Indirect Cost Data Information .....	89
9.2	Processing of Cost Data .....	90
9.2.1	Adjustment for Inflation of Capital and Operating Costs .....	91
9.2.2	Power Curves .....	96

---

9.3	Further Rules-of-Thumb .....	99
9.3.1	Rules-of-Thumb for Capital Costs .....	99
9.3.2	Rules-of-Thumb for Operating Costs .....	101
9.4	Freight Costs .....	107
9.4.1	Abbreviations in the Shipping Industry like "fob" and "cif" .....	107
9.4.2	Rules-of-Thumb for Freight Costs .....	109
<b>10</b>	<b>Additional Economic Planning Methods .....</b>	<b>113</b>
10.1	Calculation of Cutoff Grades .....	113
10.1.1	Normal Case of an Operating Cost Cutoff .....	113
10.1.2	Cutoff Calculations for Open Pits .....	114
10.2	Linear Optimization .....	117
<b>11</b>	<b>Economic Evaluations .....</b>	<b>123</b>
11.1	Static Methods .....	123
11.1.1	Profitability Quotient .....	123
11.1.2	Calculation of Rent .....	124
11.1.3	Payback Period .....	125
11.2	Dynamic Methods .....	126
11.2.1	Introduction .....	126
11.2.2	Elements of Cash Flow Calculations .....	127
11.2.3	Net Present Value (NPV) .....	130
11.2.4	The Internal Rate of Return (IRR or IROR) .....	138
11.3	Aspects of Taxation .....	145
11.3.1	Introduction .....	145
11.3.2	Depreciation .....	146
11.3.3	Depletion Allowances .....	147
11.4	Equity and Debt Financing .....	147
11.5	Example of a Cash Flow Calculation .....	148
11.6	The Concept of Profit .....	153
11.7	Sensitivity Analysis .....	154
11.8	Breakeven Calculations .....	157
11.8.1	Breakeven Calculations for Mono-Metallic Deposits .....	157
11.8.2	Breakeven Calculations for Multi-Element Deposits .....	158
11.9	The Expected Monetary Value (EMV) Method .....	160
11.10	The Option Pricing Method .....	162
11.10.1	Mine Production As an Option on Future Delivery .....	165
11.10.2	Assessing Undeveloped Properties by Option Pricing .....	166
11.11	Dealing with Start-up Problems in Economic Evaluations .....	168
<b>12</b>	<b>Quantitative Valuation of Exploration Projects without Known Mineralization .....</b>	<b>171</b>
12.1	Introduction .....	171
12.2	Valuation of Properties without Known Exploitable Reserves .....	171

<b>13 Comparison of Deposits .....</b>	175
13.1 Comparison of Deposits Via the Metal Content .....	175
13.2 The Borderline of Viability .....	178
13.3 The Breakeven Curve in a Grade-Capacity Diagram .....	179
13.4 Grade-Capacity Diagram with Lines of Equal Economic Parameters .....	181
13.5 Comparison of Deposits with Cost Charts .....	184
13.6 Comparison of Deposits with Auxiliary Criteria .....	184
<b>14 Calculating Growth Rates .....</b>	185
14.1 Calculating Growth Rates Using the Geometrical Mean .....	185
14.2 Calculating Growth Rates with Logarithmic Values and Linear Regression ..	186
14.3 Doubling Periods .....	189
<b>15 Equity Calculations .....</b>	191
15.1 Equity Calculations with Several Partners .....	191
15.2 Calculation of Foreign Equity in Exploration and Mining Projects .....	193
<b>References .....</b>	197
<b>Appendices .....</b>	201
A Diagrams for Conversion between Imperial and Metric Units .....	201
B Diagrams to Determine the Thickness Reduction Factors for Drilling Oblique to Strike and Dip at Different Angles of Inclination and Diagram to Determine the Optimal Angle of Inclination of Drill Holes for Drilling Oblique to Strike .....	206
C Part 1 · Derivation of the Formula for Calculating a Density Equivalent of Sect. 3.5.3 .....	209
Part 2 · Spreadsheet to Calculate Densities of Complex Ore .....	211
D Tables .....	212
E Problems Created by the Application of Geometrical Series .....	228
F Sources of Information, Internet Addresses, Abbreviations, Conversions ..	230
G Scales (for the Field Book) .....	235
<b>Index .....</b>	239